

# Regular Model Checking without Transducers

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# This Presentation

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- Basic Model
- Transition System
- Safety
- Monotonicity and Approximation
- Algorithm and Results
- Conclusion

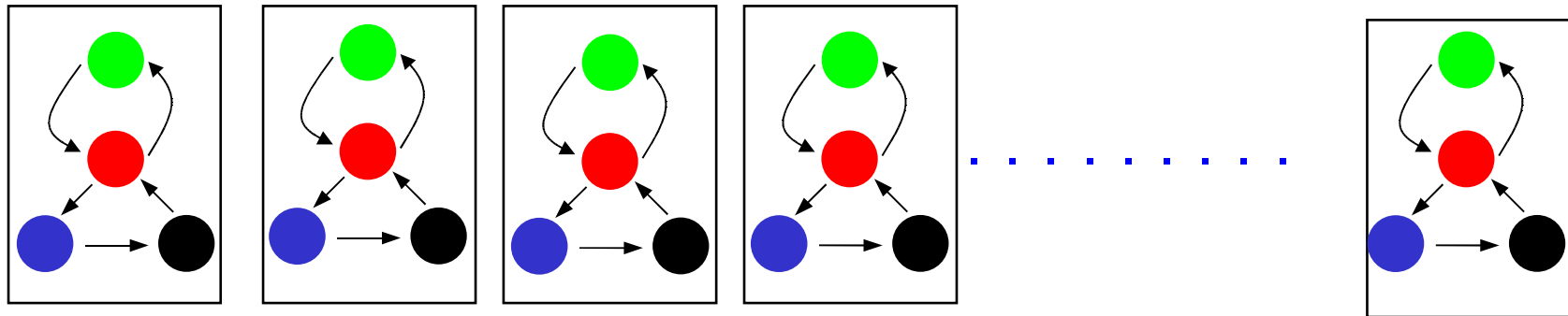
# This Presentation

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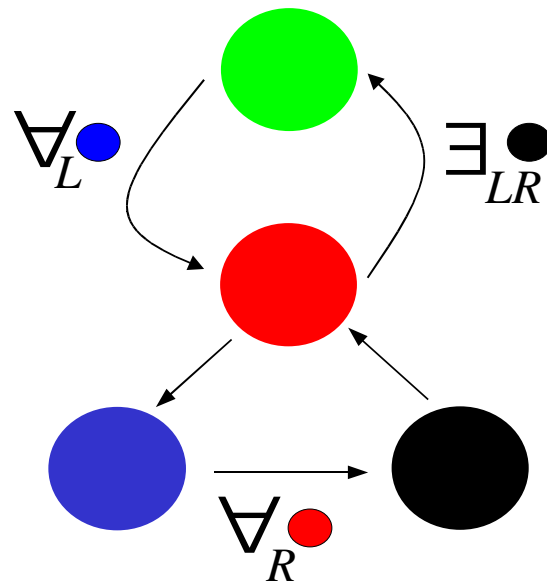
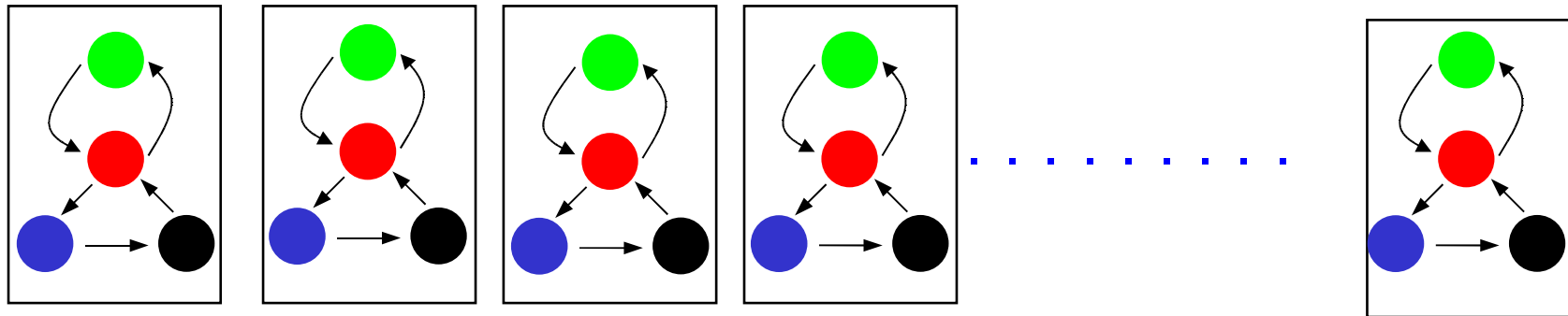
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# Basic Model

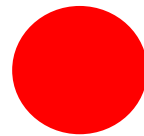
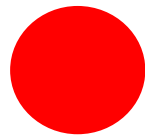
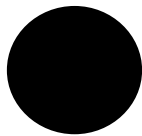
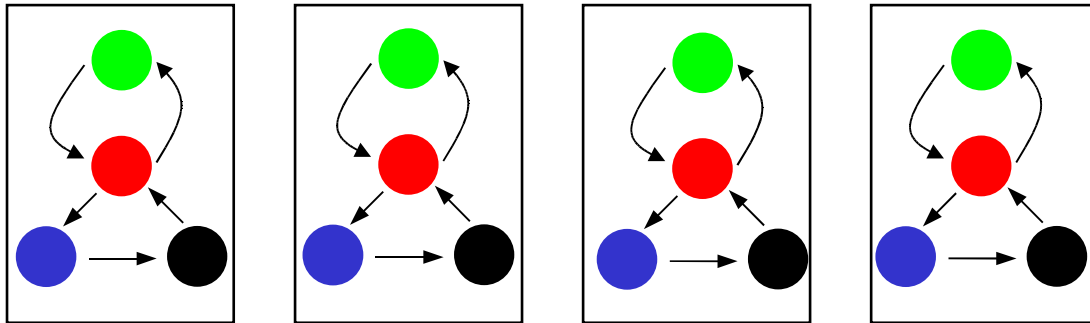
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# Basic Model



# Transition Systems

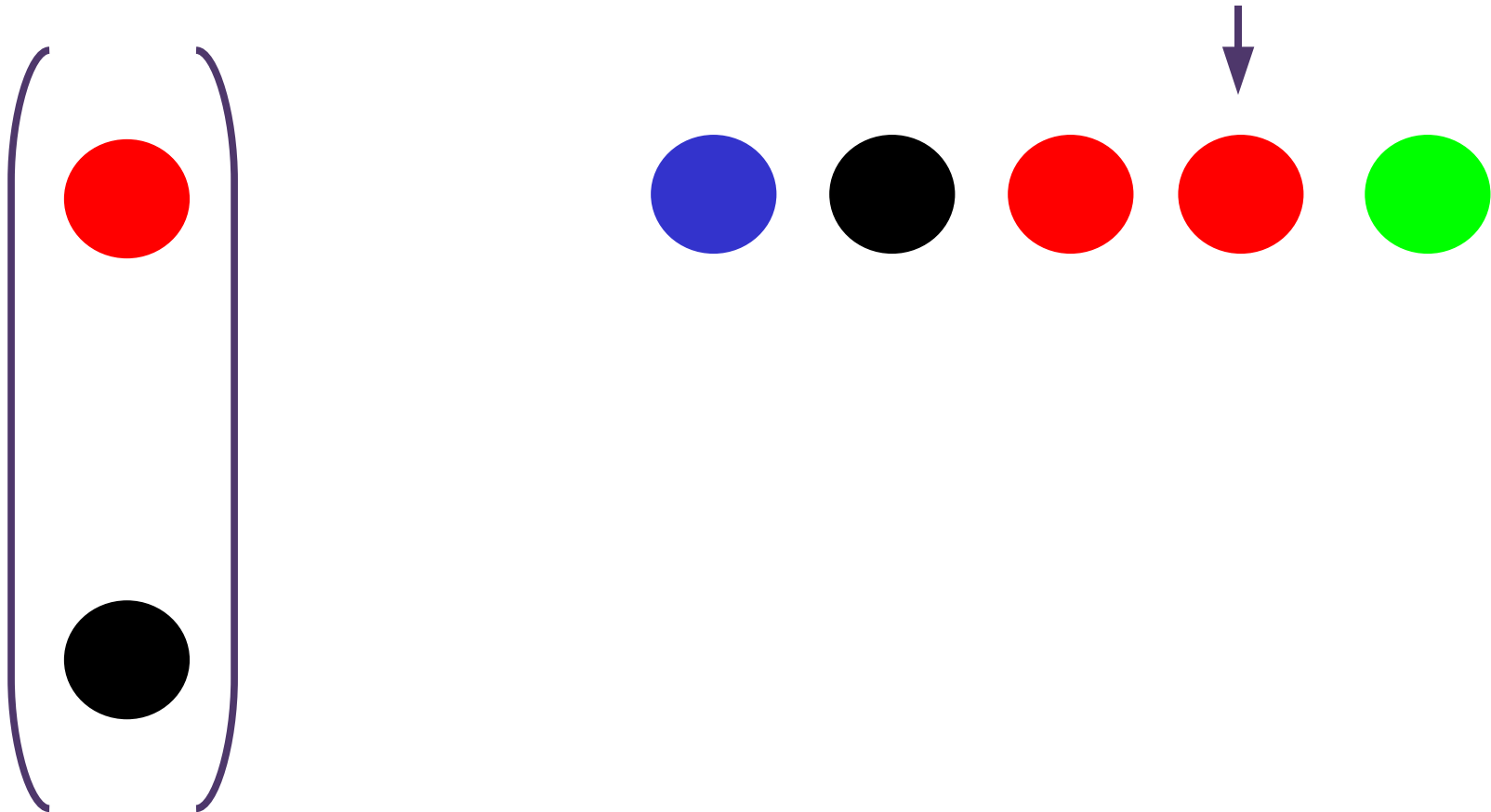


Configuration

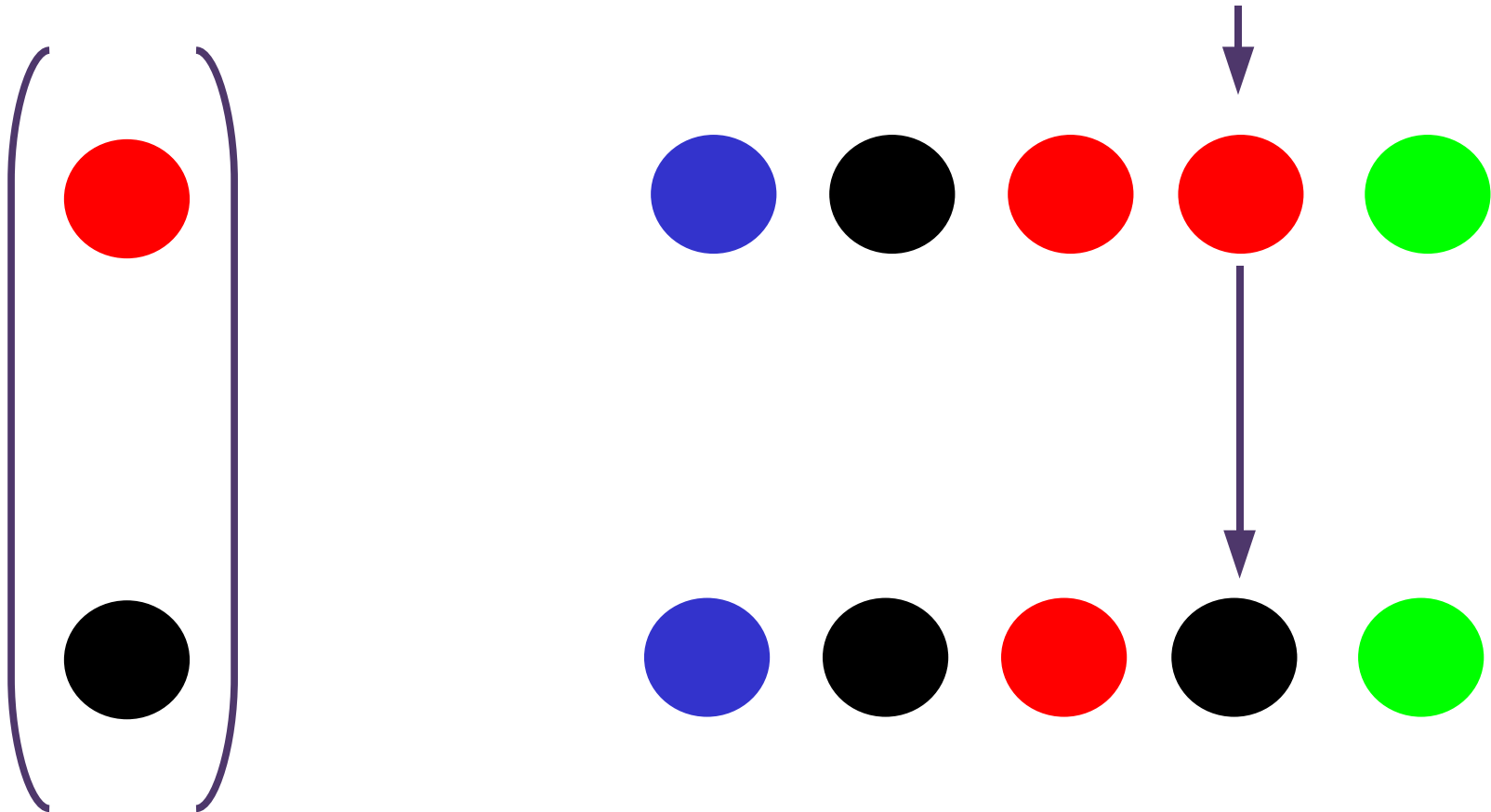


# Transitions : Local

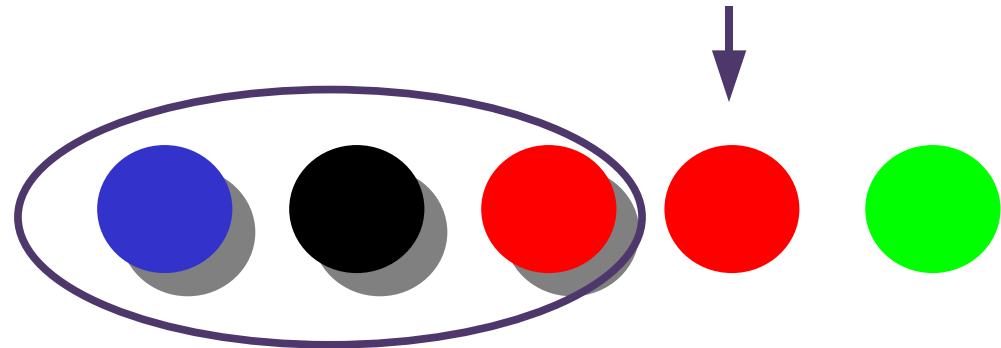
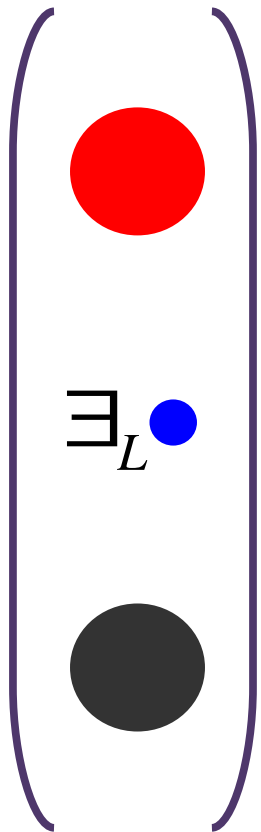
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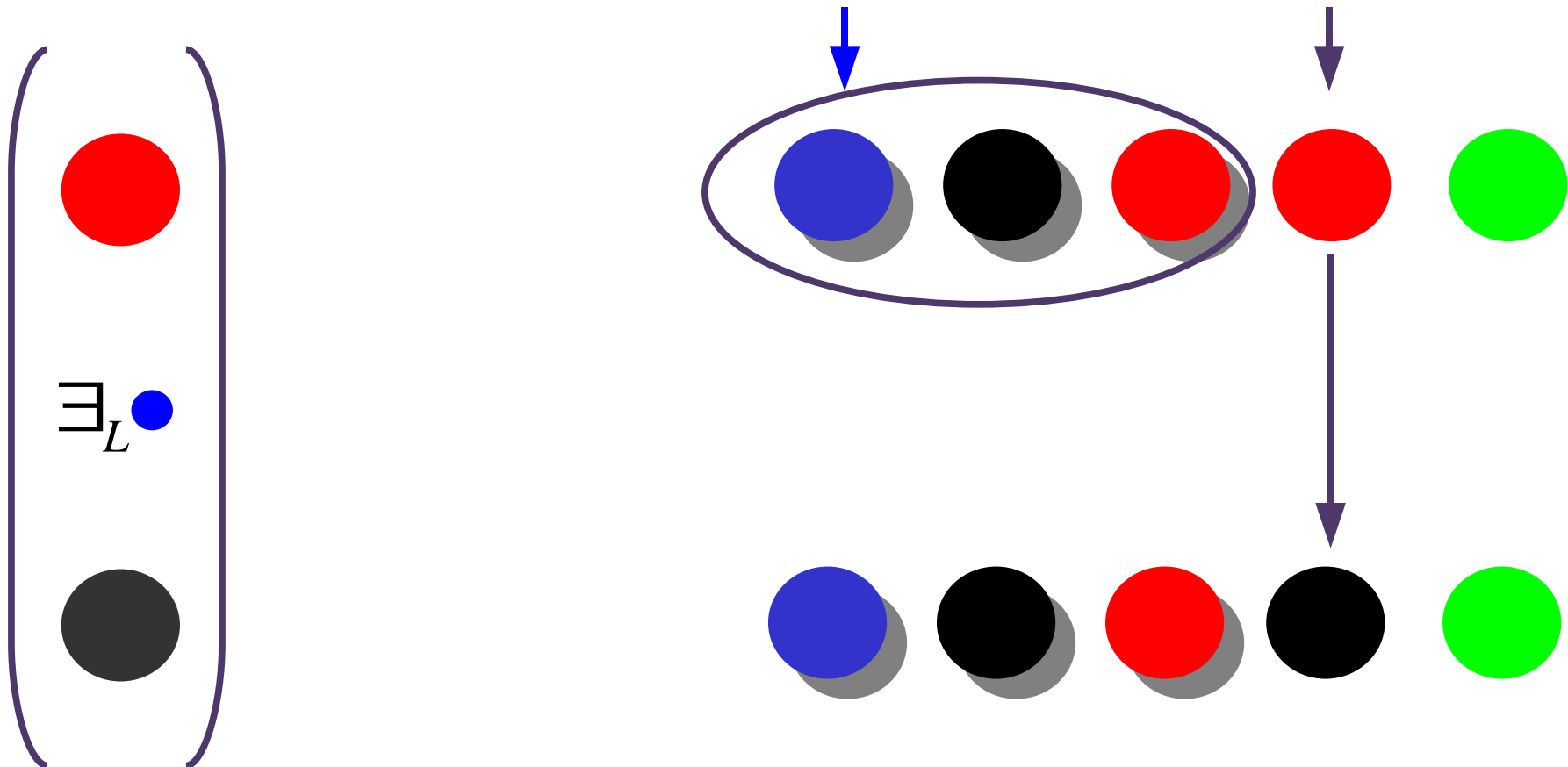
# Transitions : Local



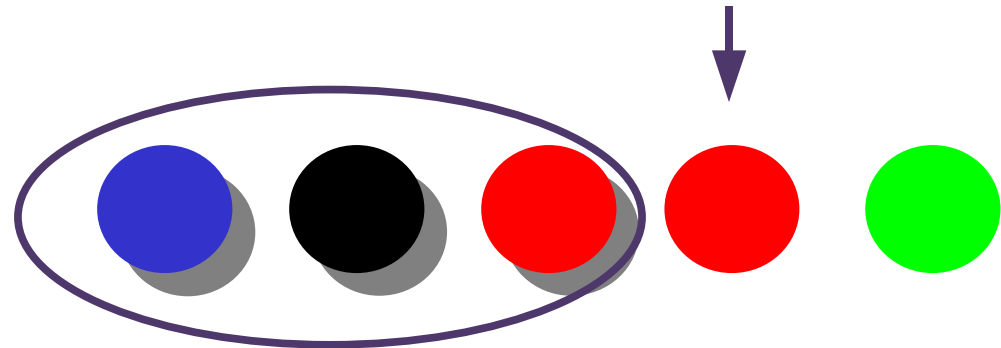
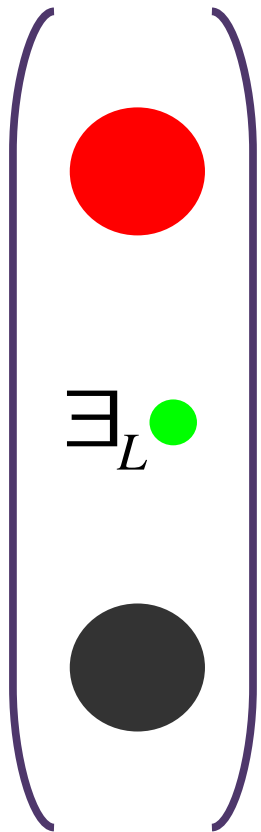
# Transitions : Existential



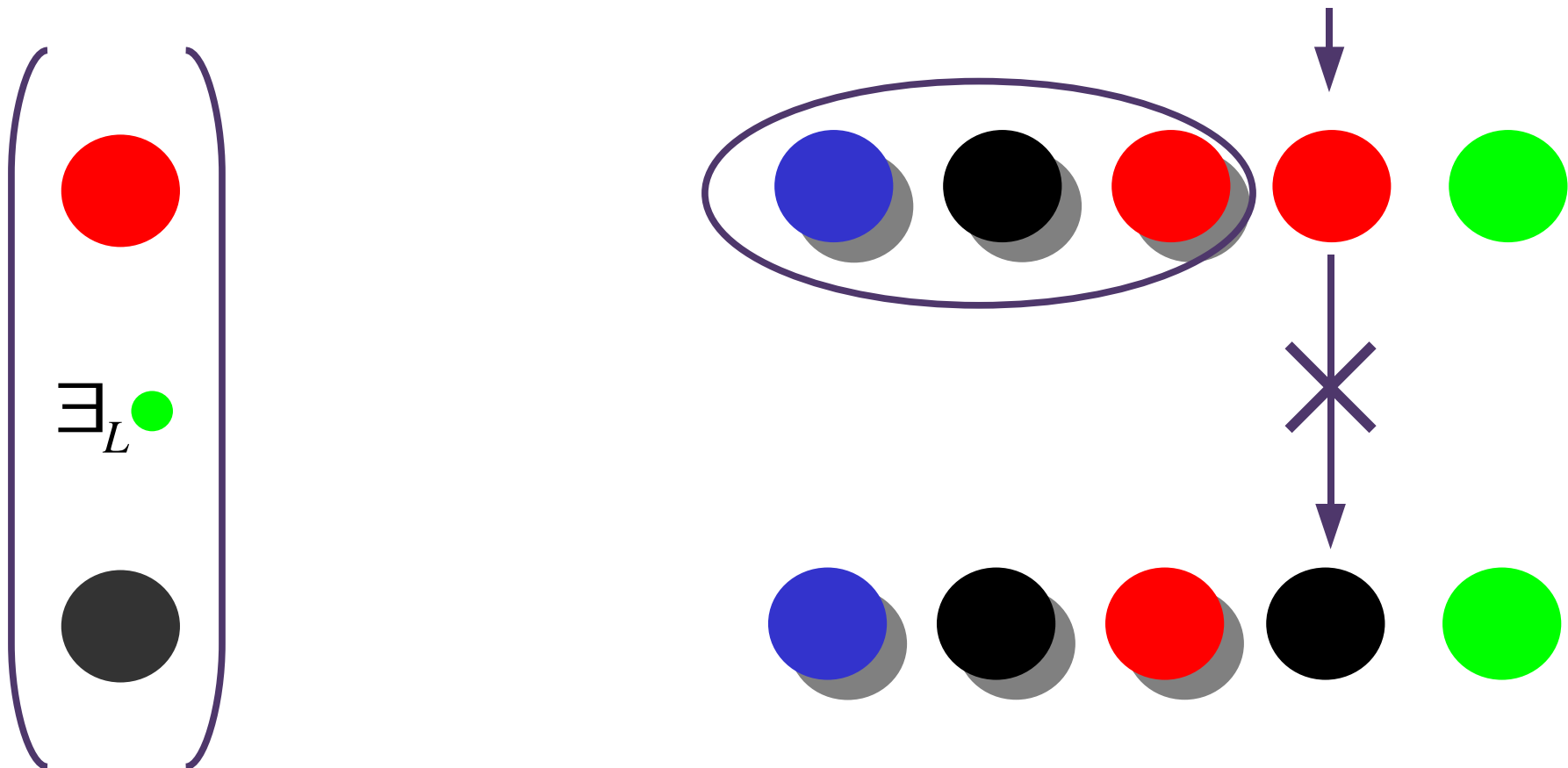
# Transitions : Existential



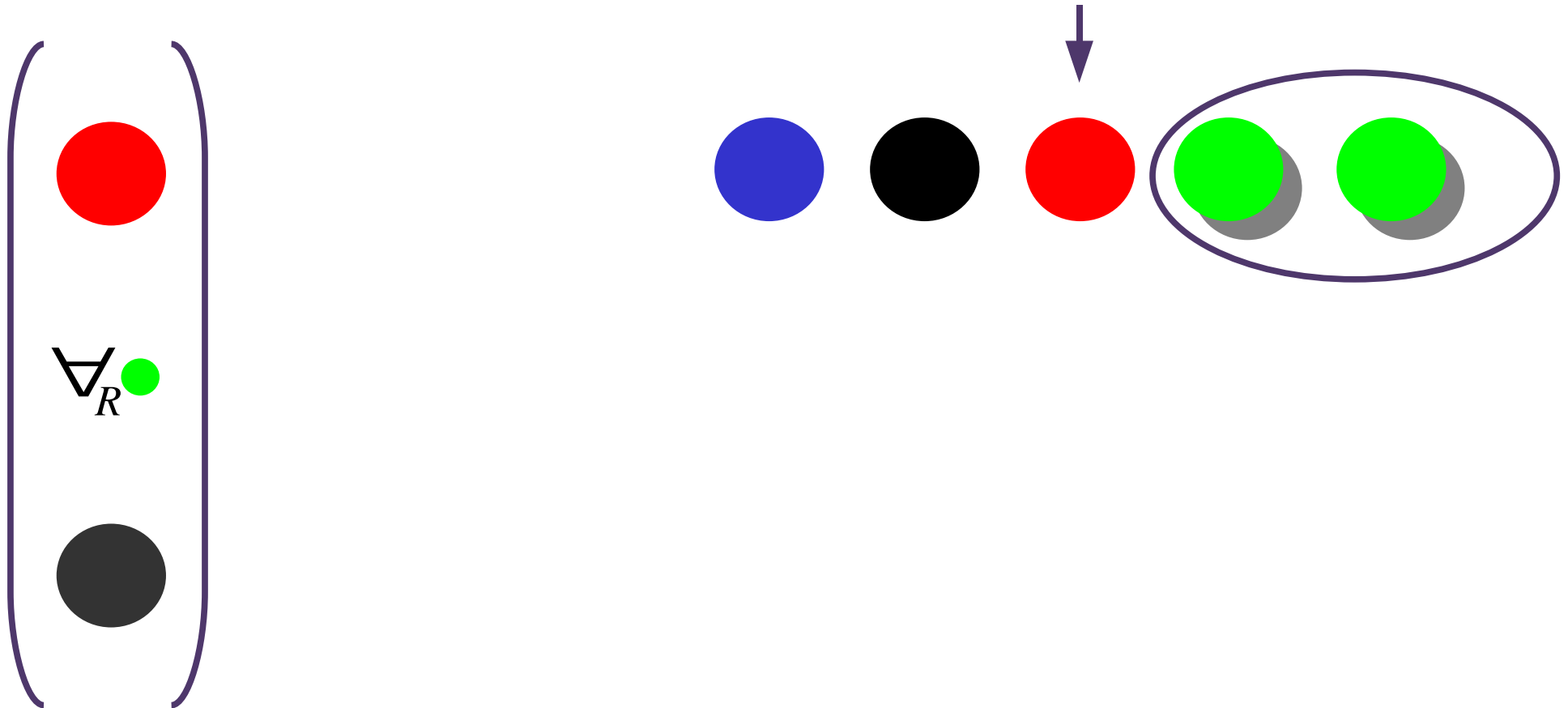
# Transitions : Existential



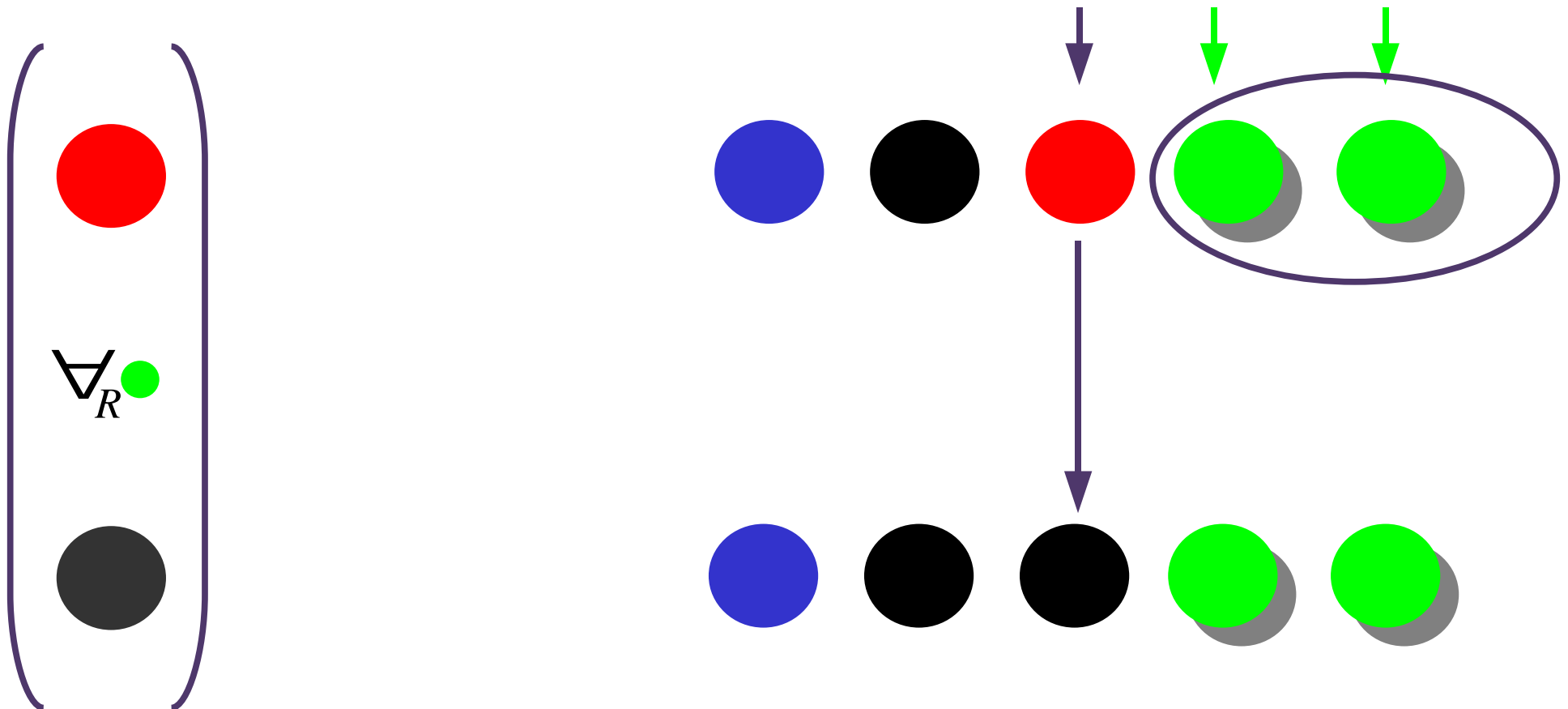
# Transitions : Existential



# Transitions : Universal

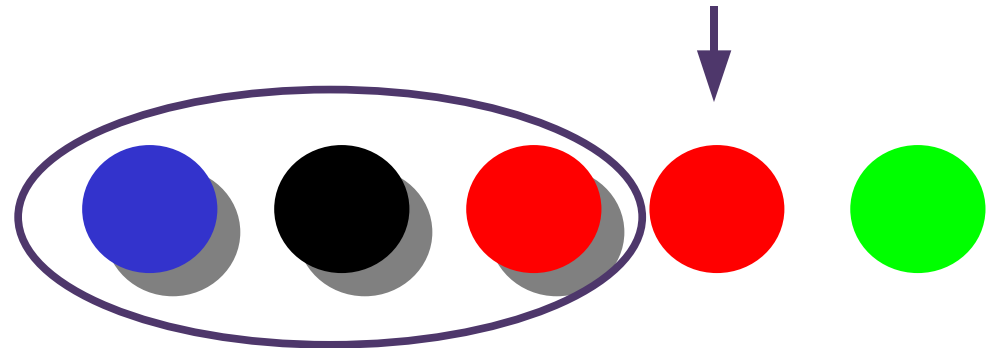
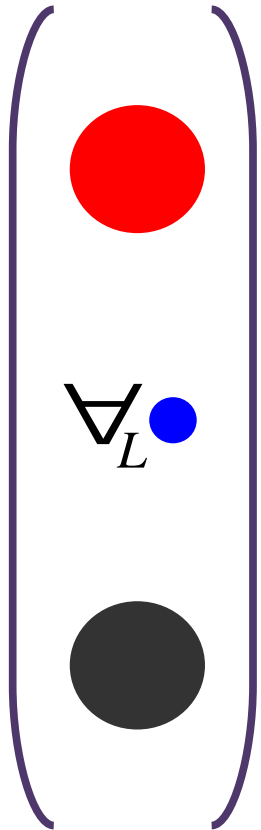


# Transitions : Universal

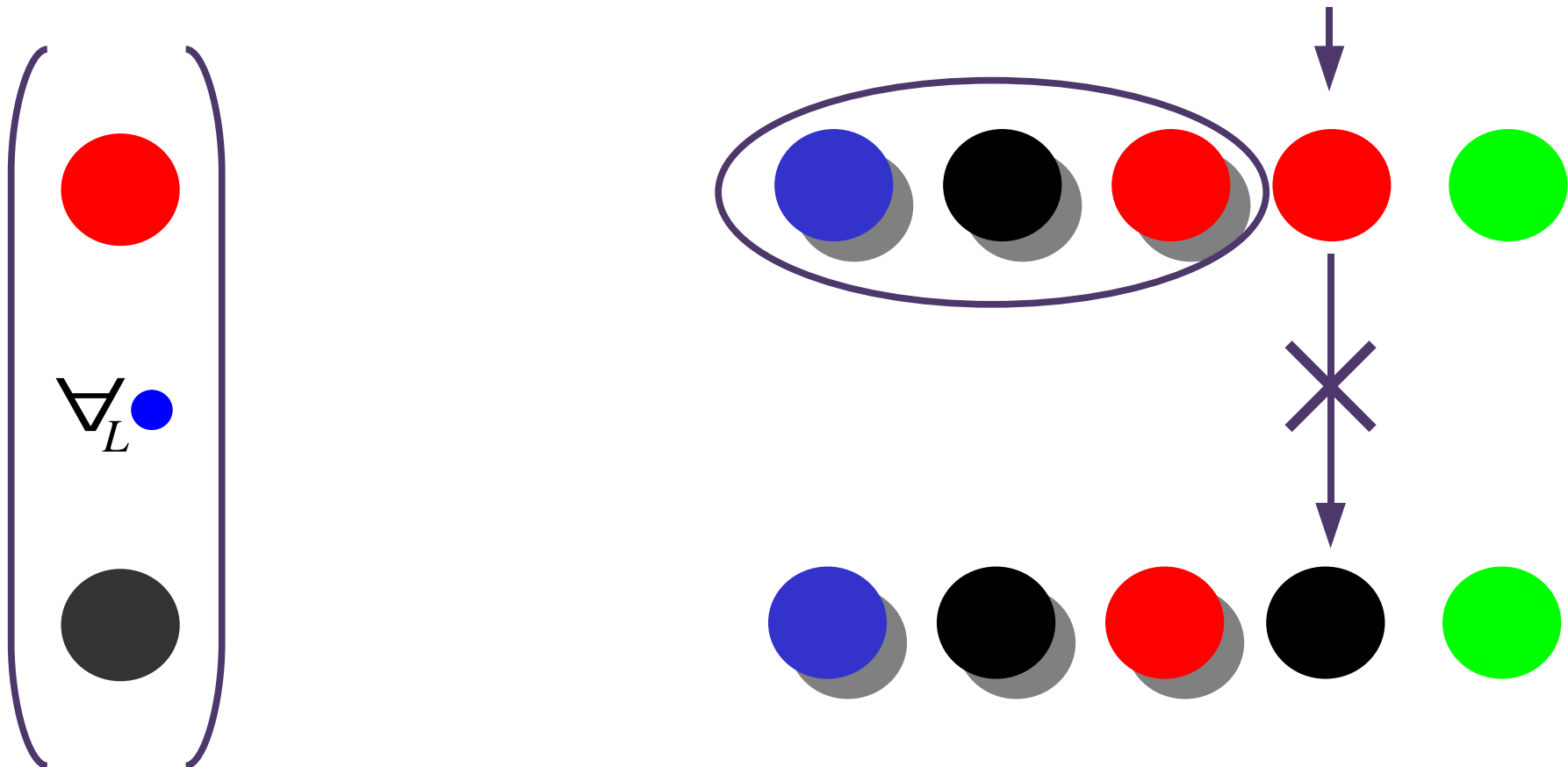




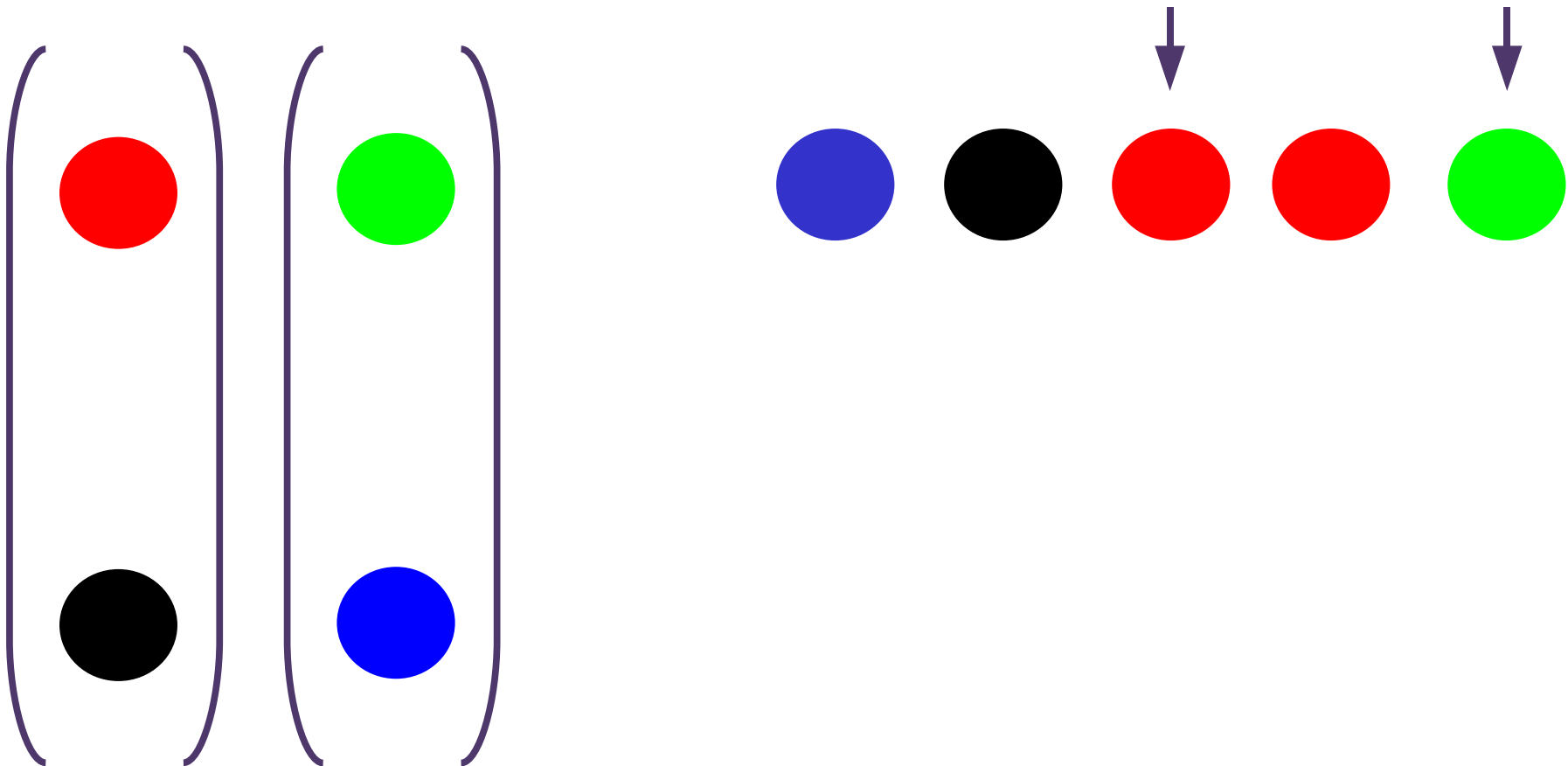
# Transitions : Universal



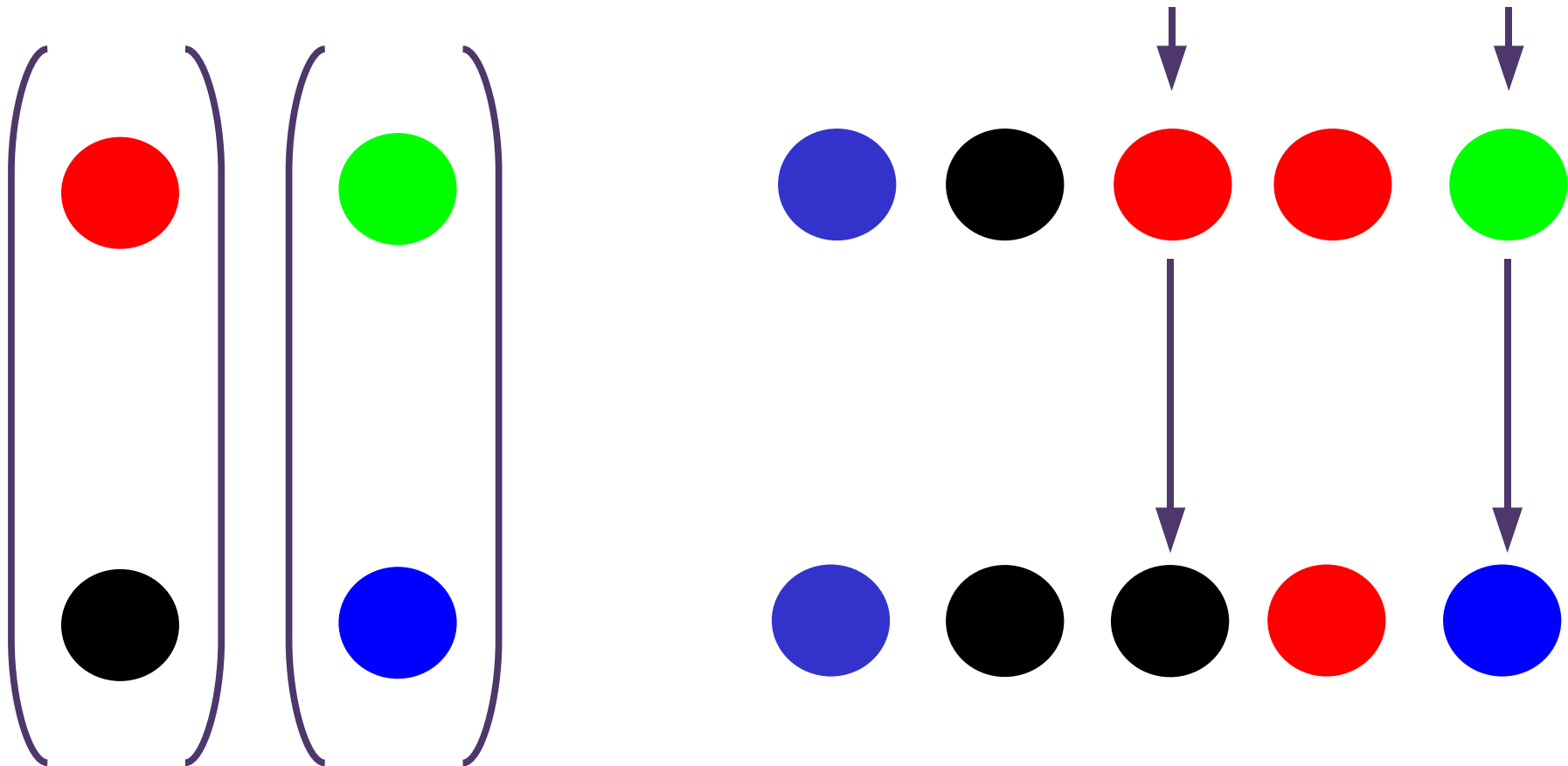
# Transitions : Universal



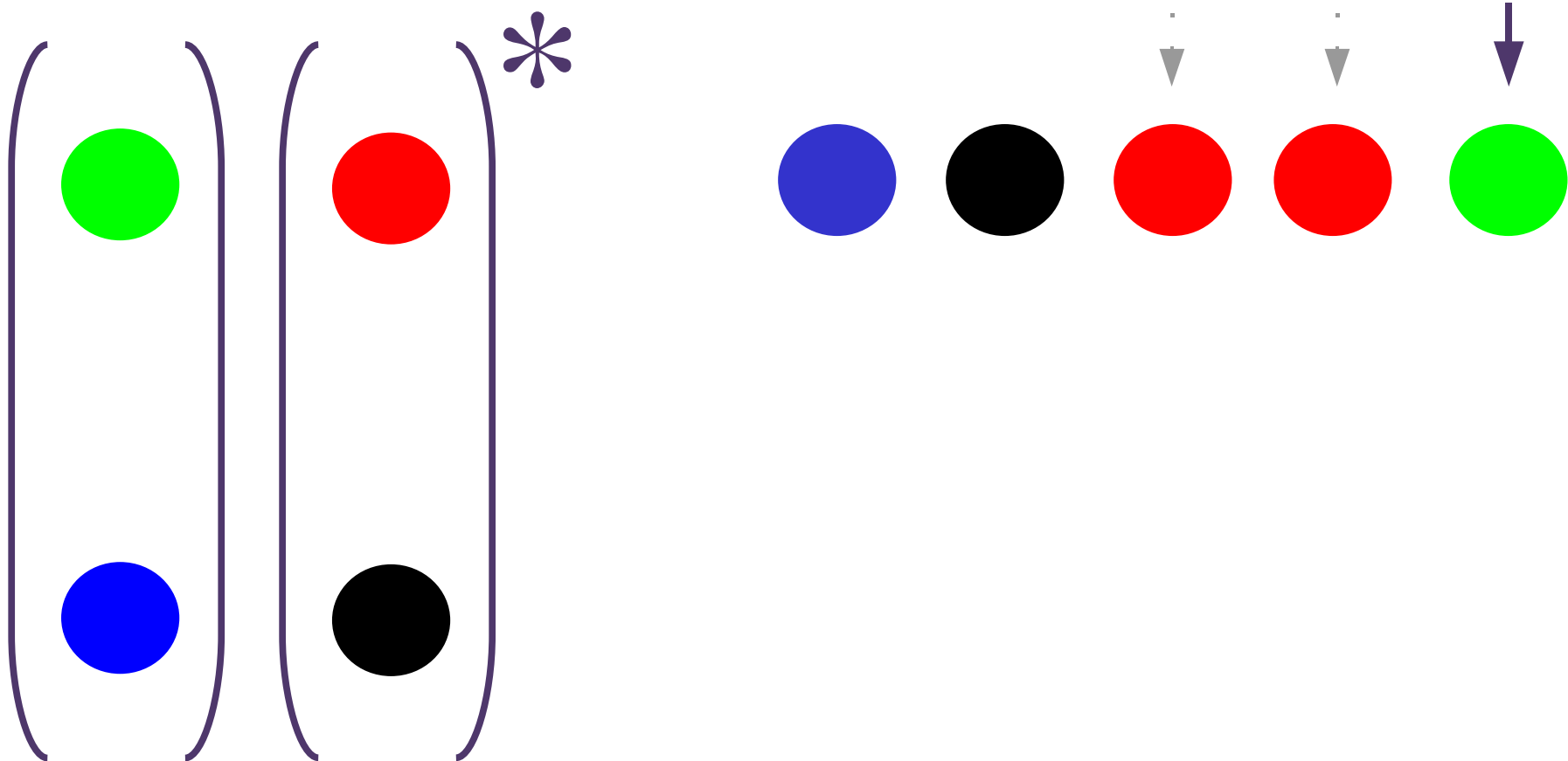
# Transitions : Binary Communication



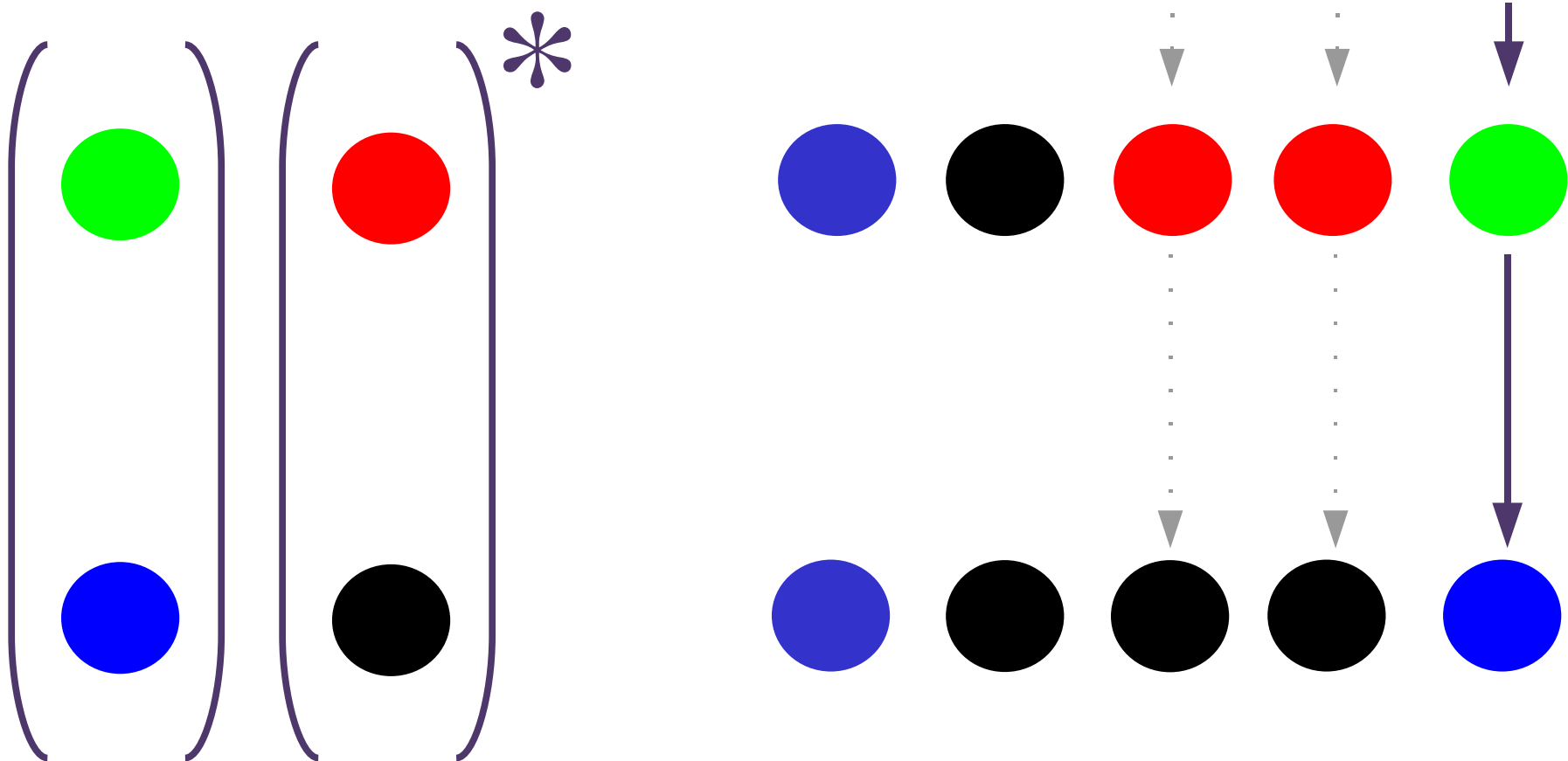
# Transitions : Binary Communication



# Transitions : Broadcast



# Transitions : Broadcast



## Examples

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- Mutual exclusion algorithms by:  
Burns, Szymanski, Dijkstra ...
- Cache coherence protocols:  
Mesi, Illinois, Futurebus, German, ...

# This Presentation

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- Basic Model
- **Transition System**
- Safety
- Monotonicity and Approximation
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# This Presentation

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# Safety

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- Reachability of bad configurations.

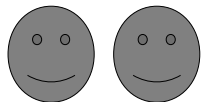
# Safety

---

- Reachability of bad configurations.



Critical Section



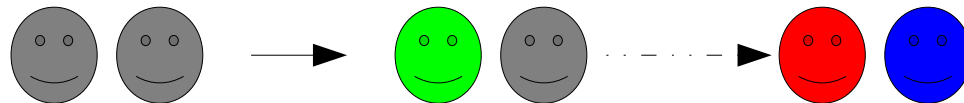
Initial

# Safety

- Reachability of bad configurations.



Critical Section



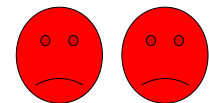
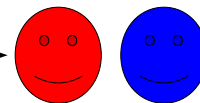
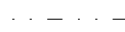
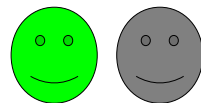
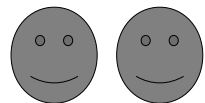
Initial

# Safety

- Reachability of a bad configuration.



Critical Section

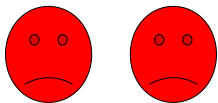


Initial

# Safety

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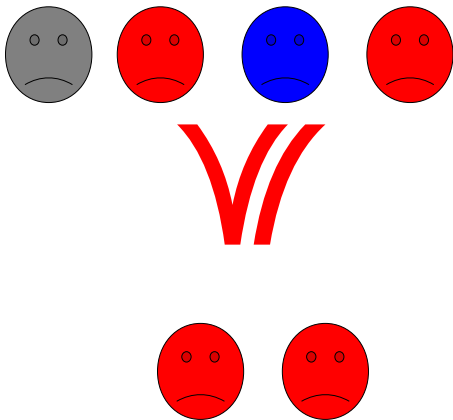
- Reachability of a bad configuration.



# Safety

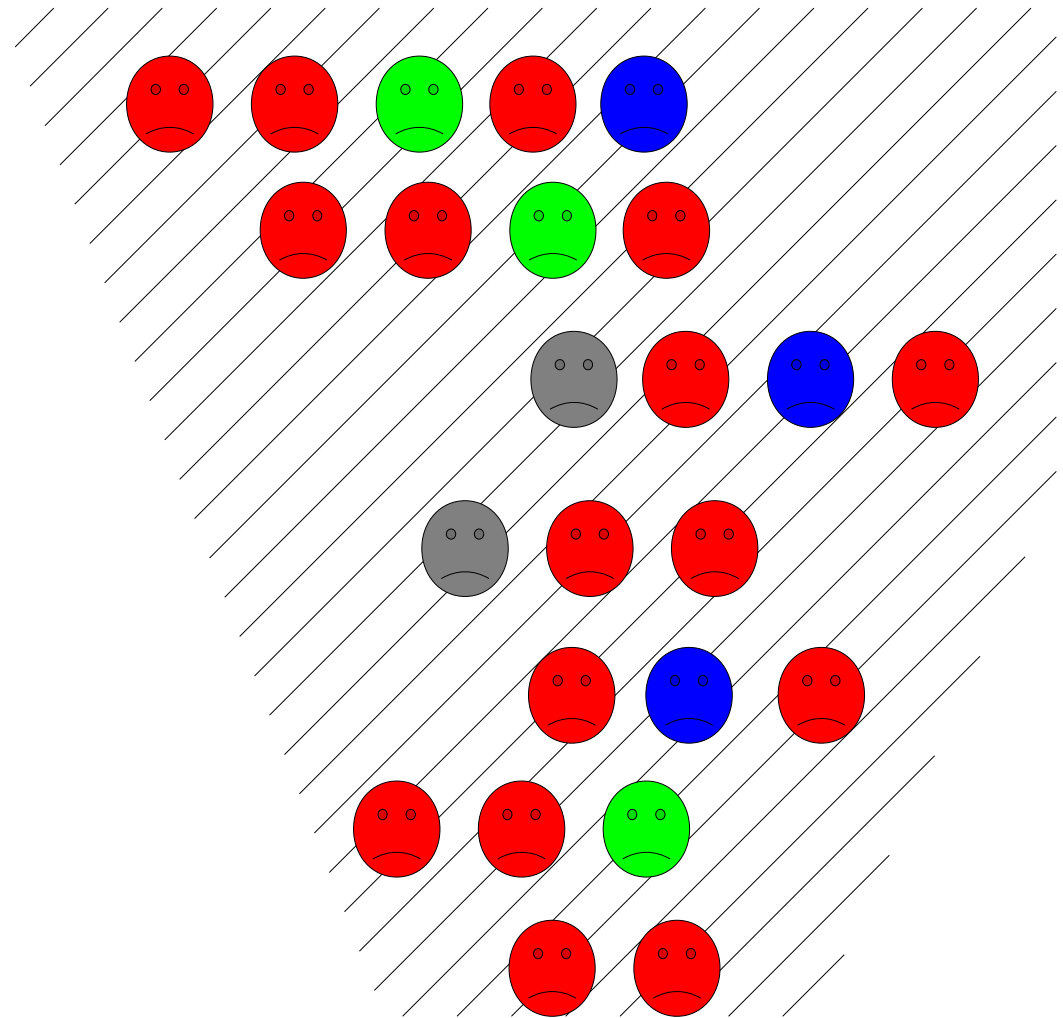
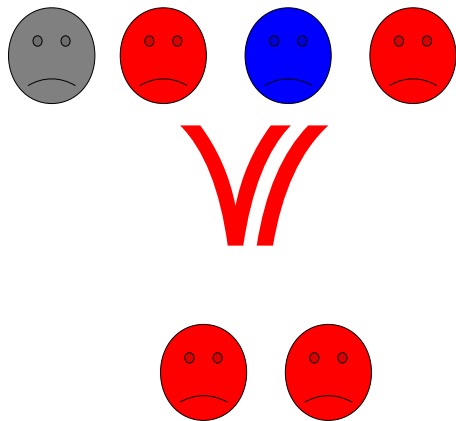
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- Reachability of a bad configuration.



# Safety

- Reachability of a bad configuration.

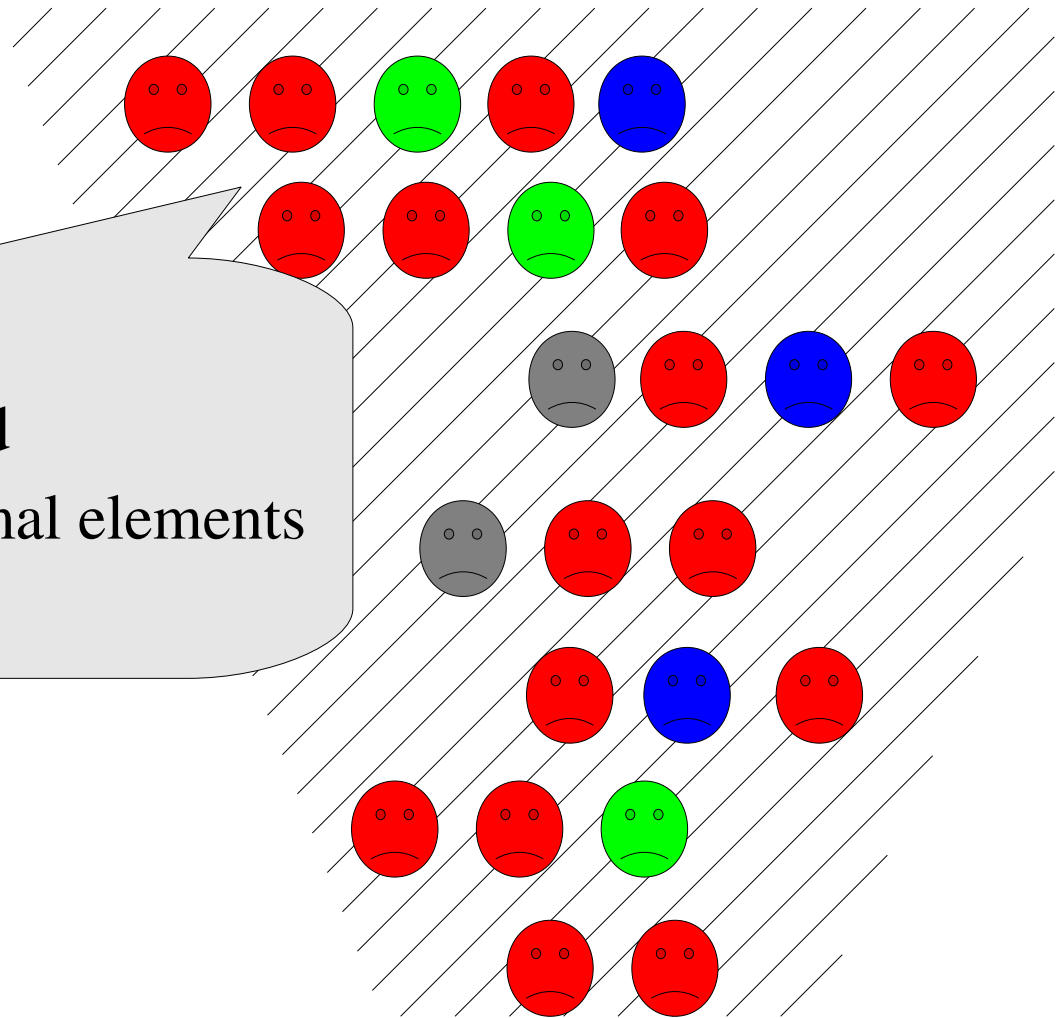
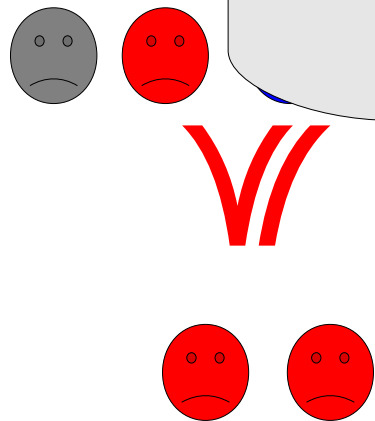




# Safety

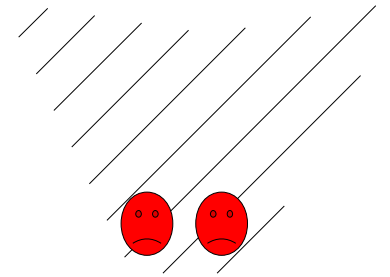
- Reachability of a bad configuration

- Bad = Upward Closed
- represented by minimal elements



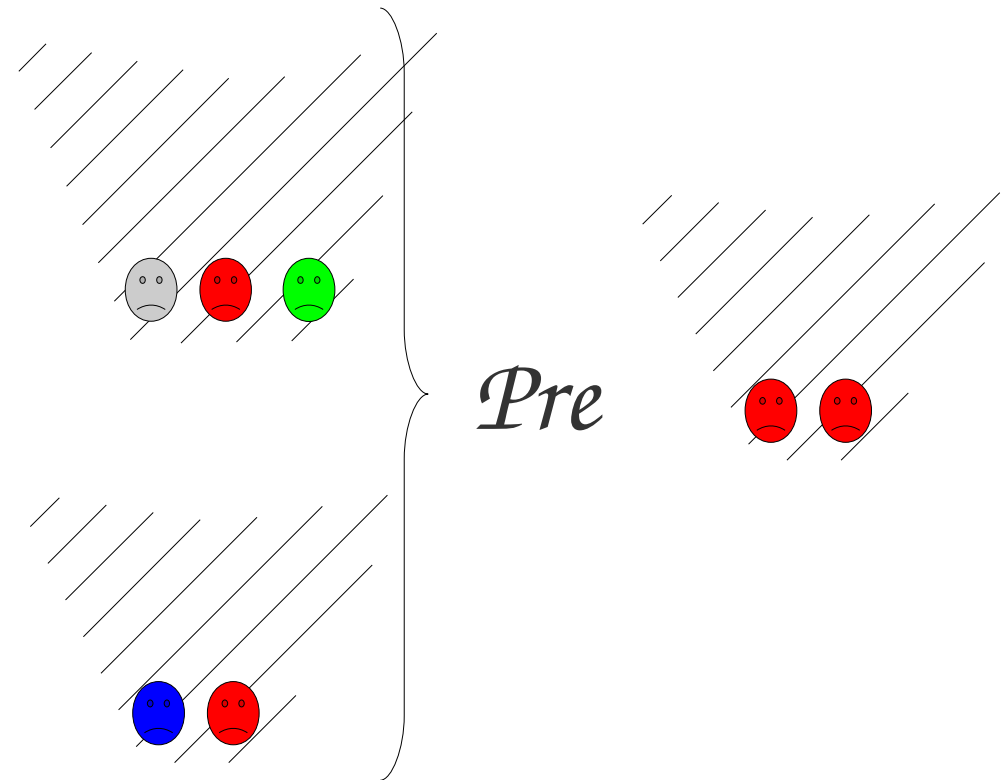
# Safety

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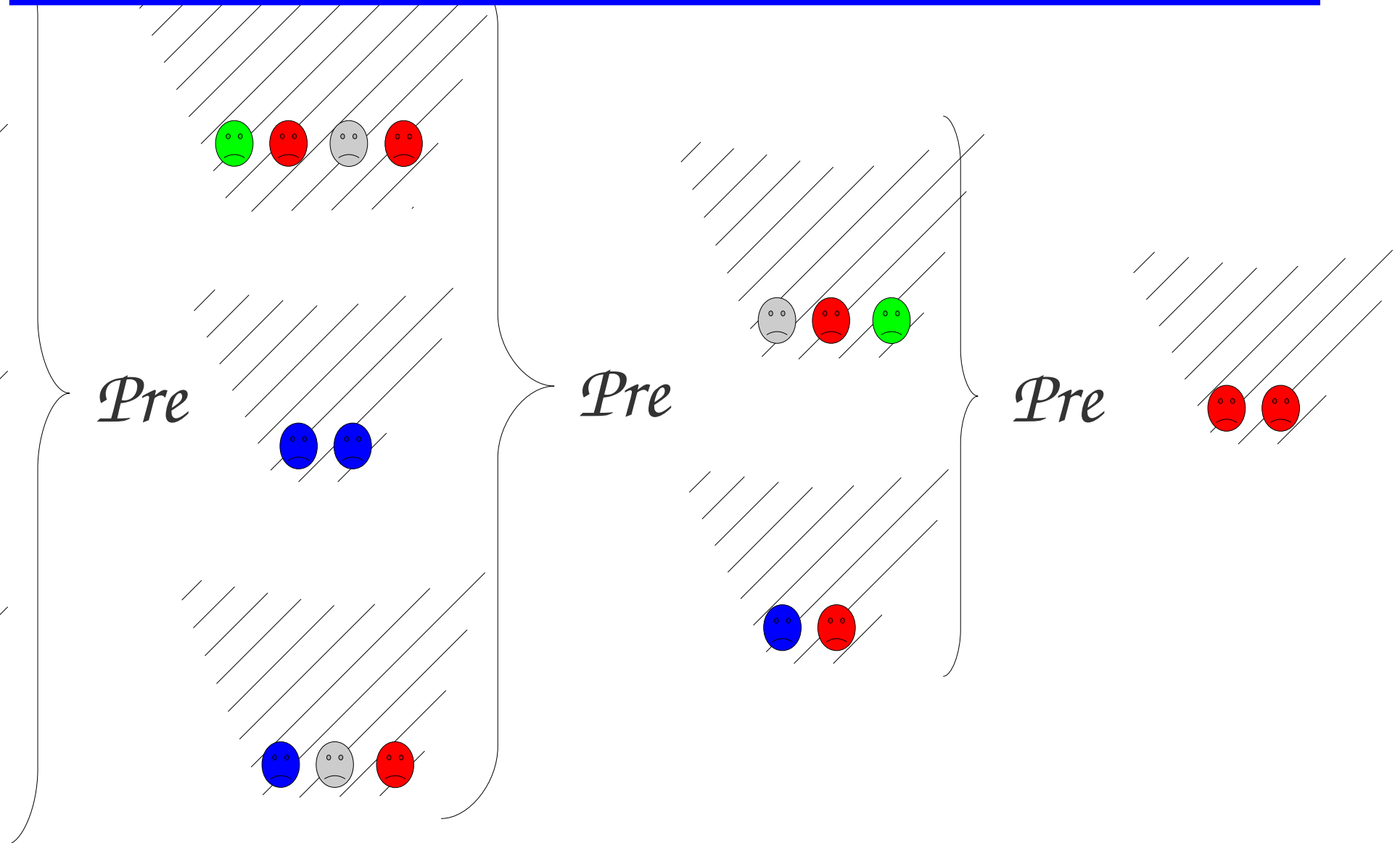


# Safety

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# Safety



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# Monotonicity

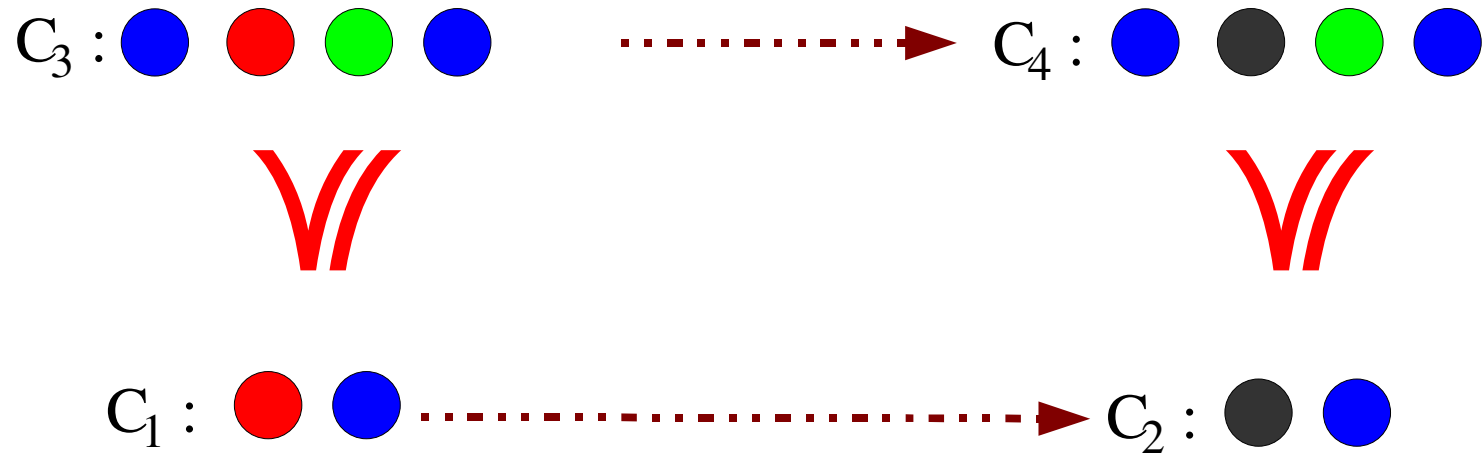
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$C_3$  : ● ● ● ●



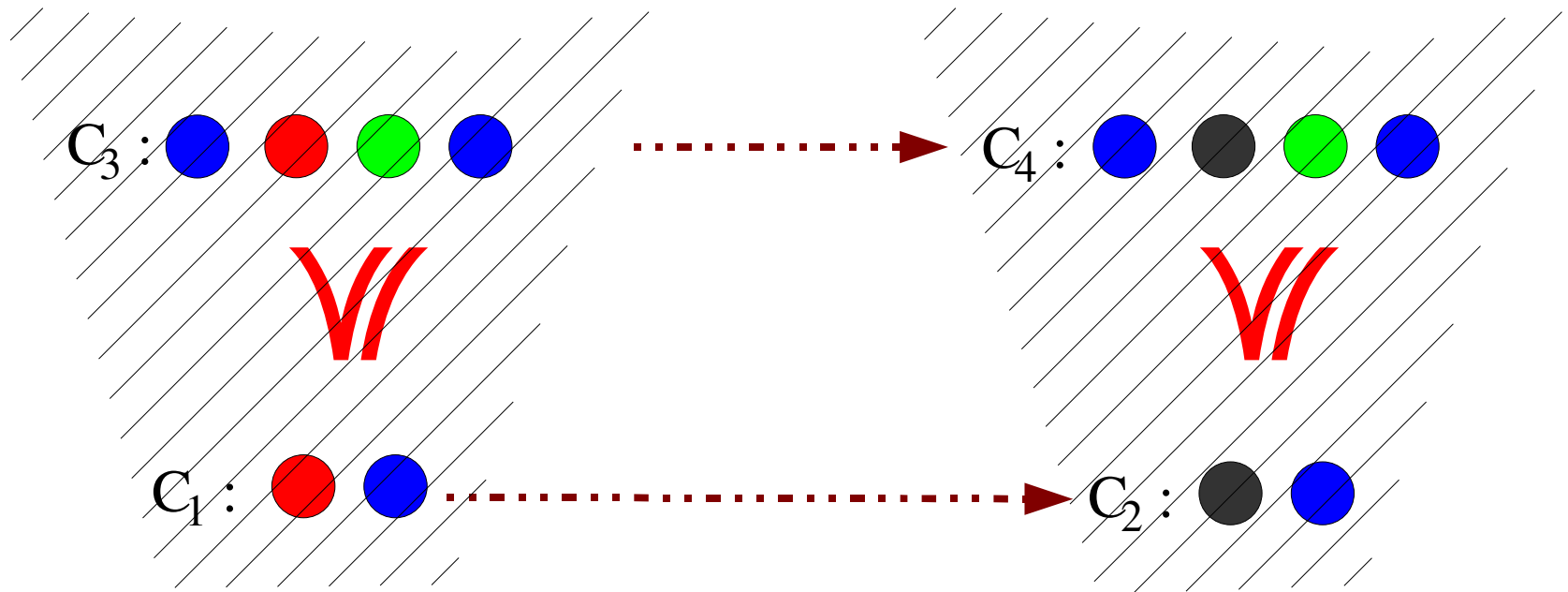
$C_1$  : ● ● .....  $C_2$  : ● ●

# Monotonicity



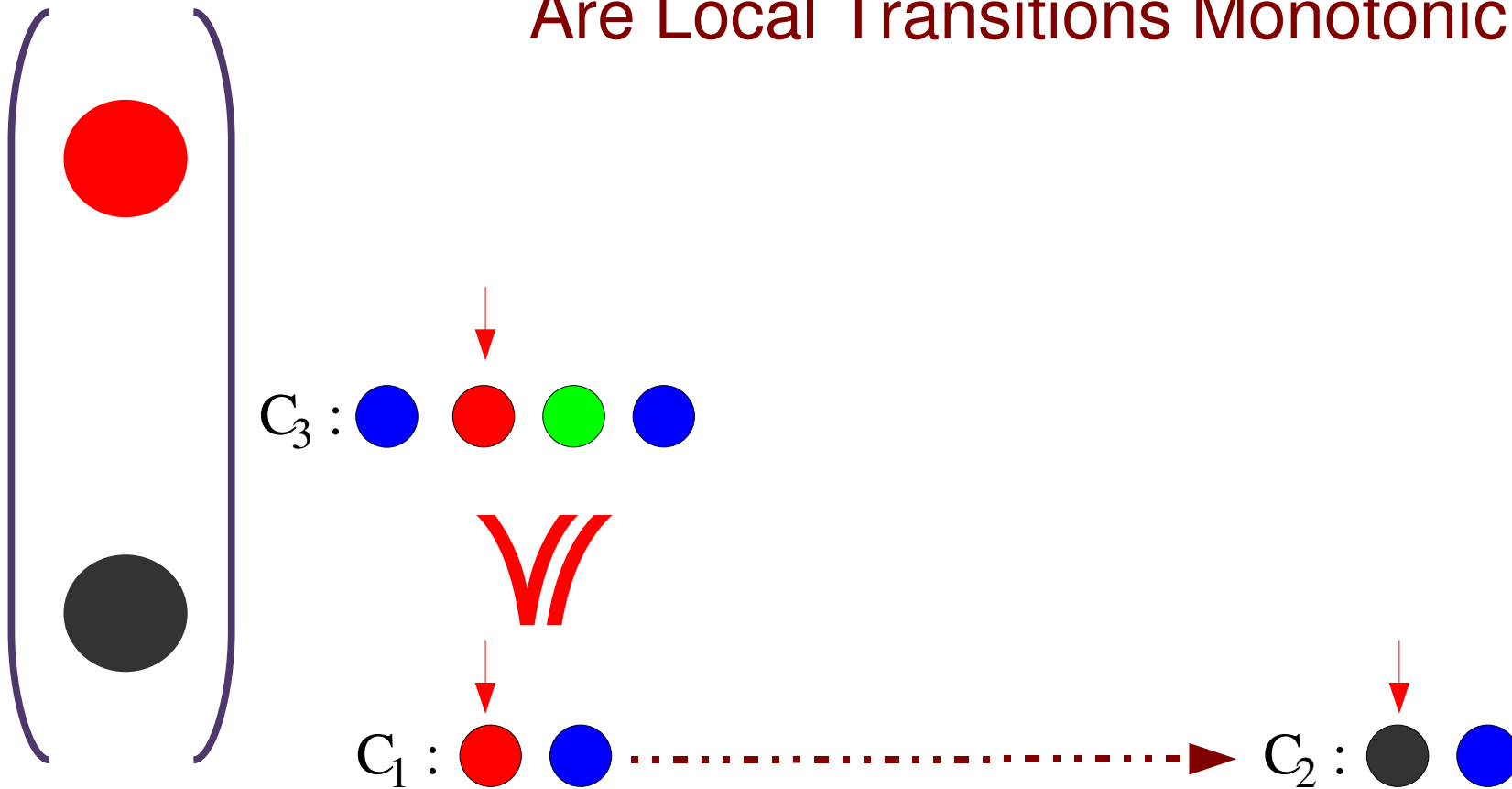


# Monotonicity



# Monotonicity

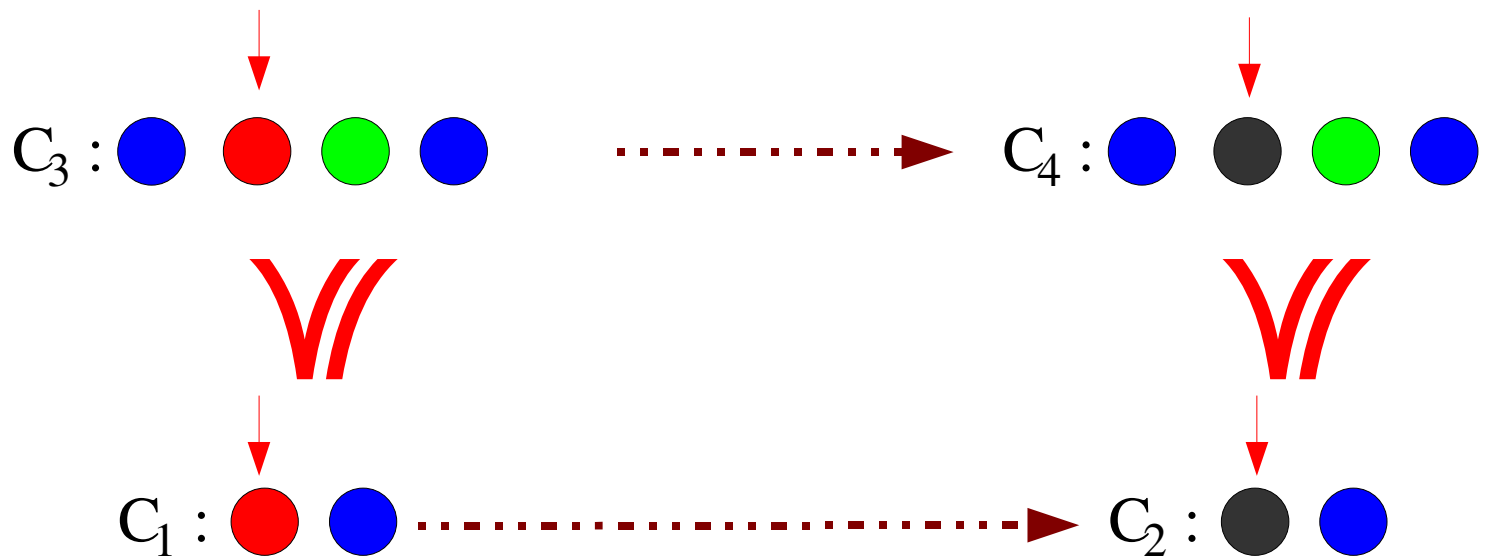
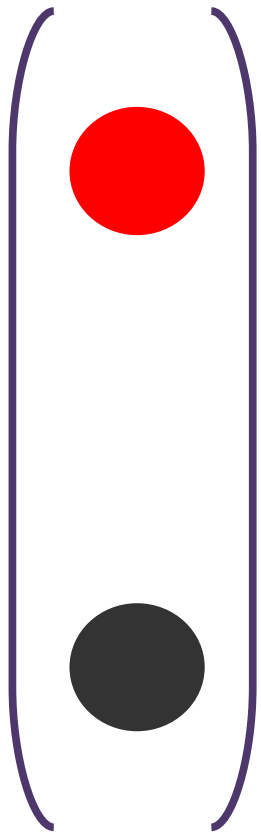
Are Local Transitions Monotonic?



# Monotonicity

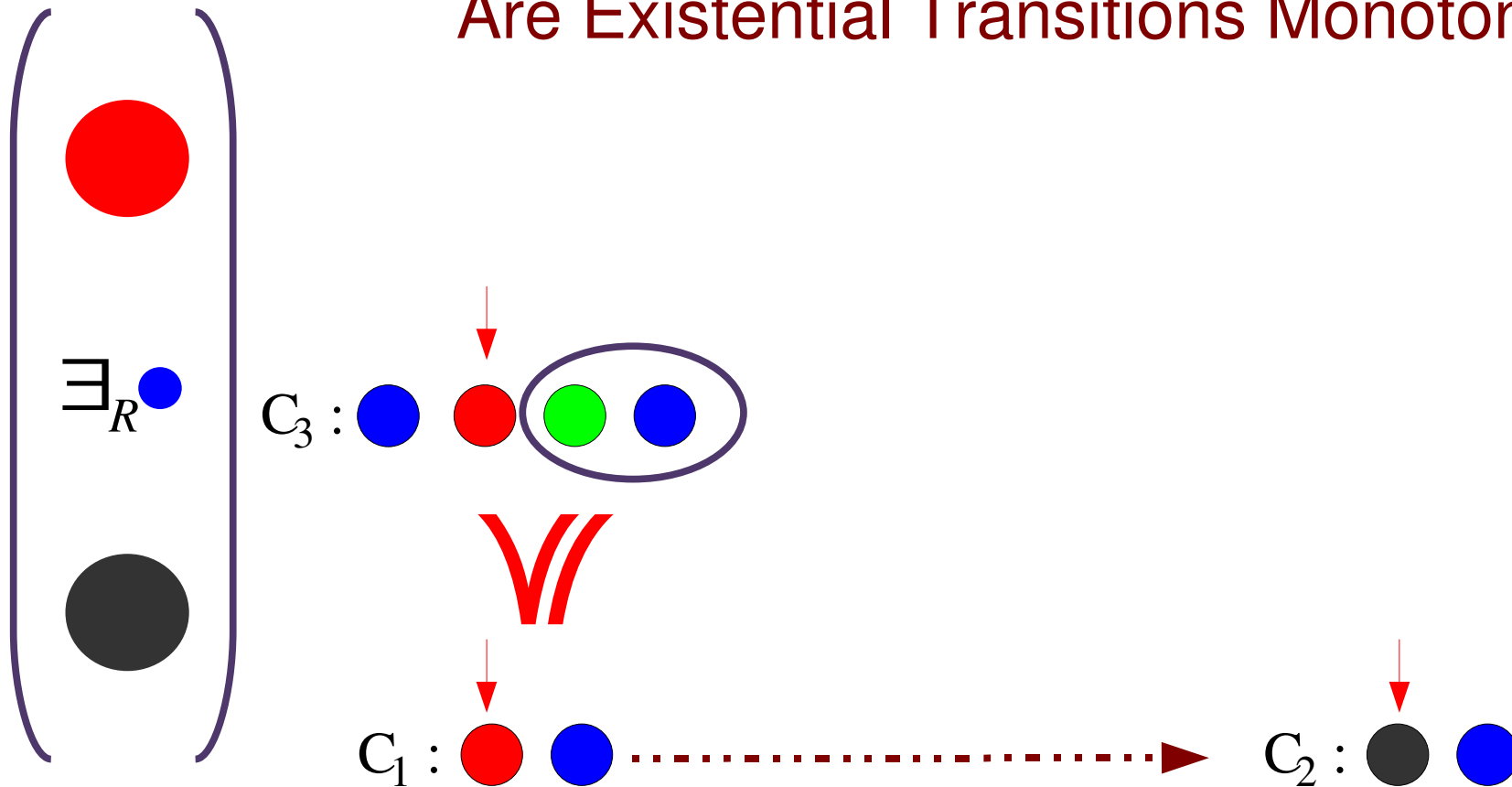
Are Local Transitions Monotonic?

YES



# Monotonicity

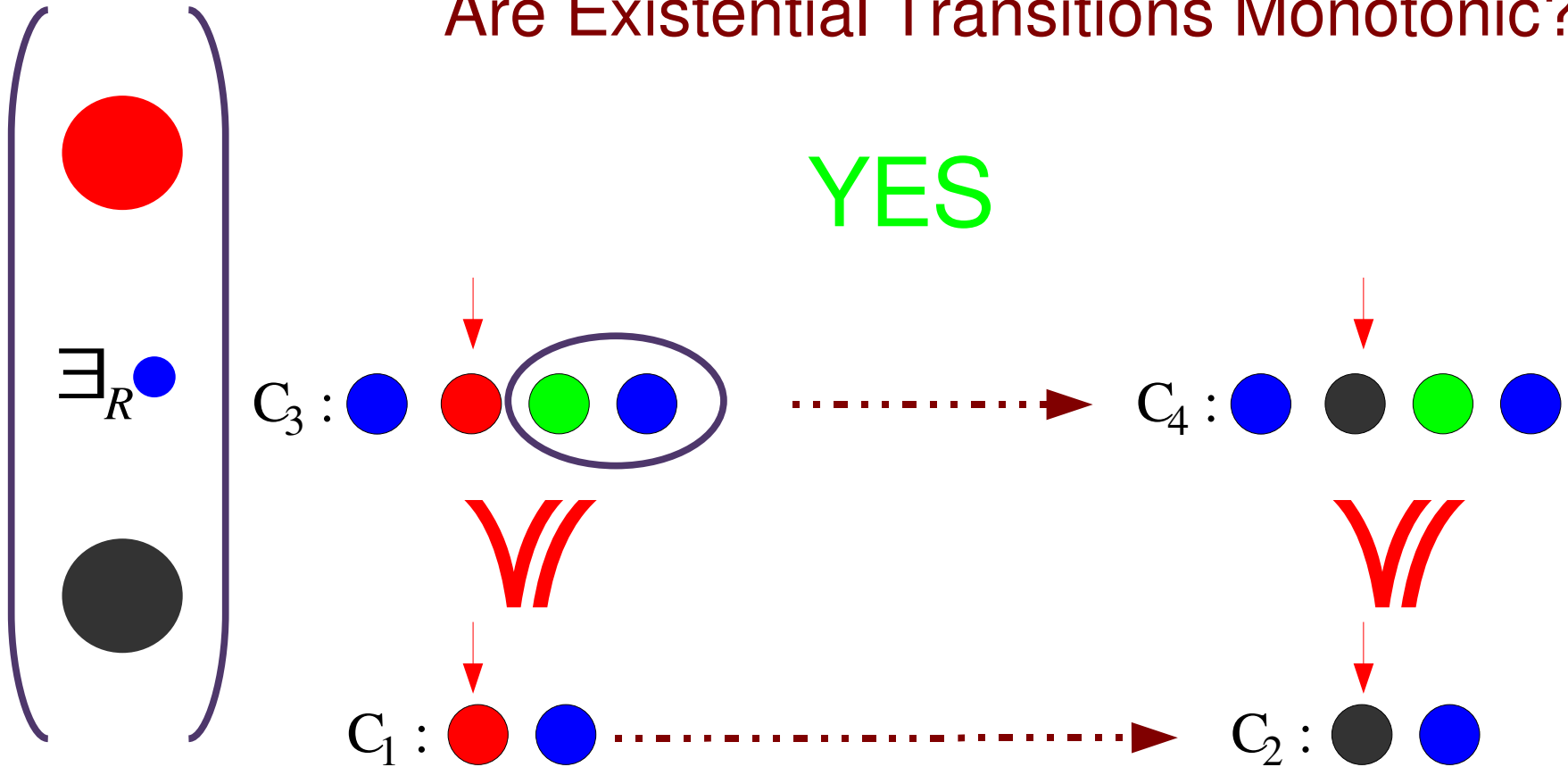
Are Existential Transitions Monotonic?



# Monotonicity

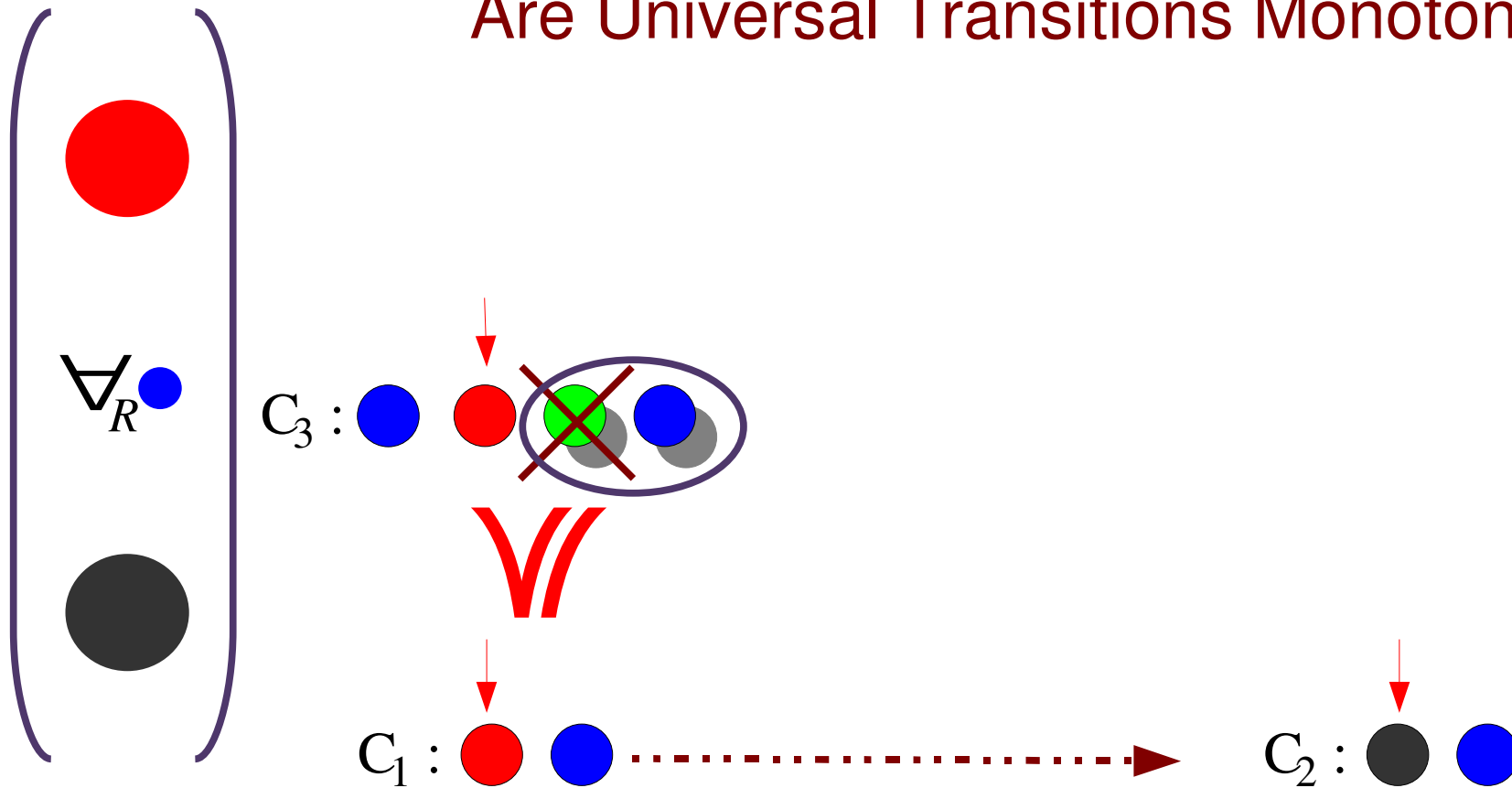
Are Existential Transitions Monotonic?

YES



# Monotonicity

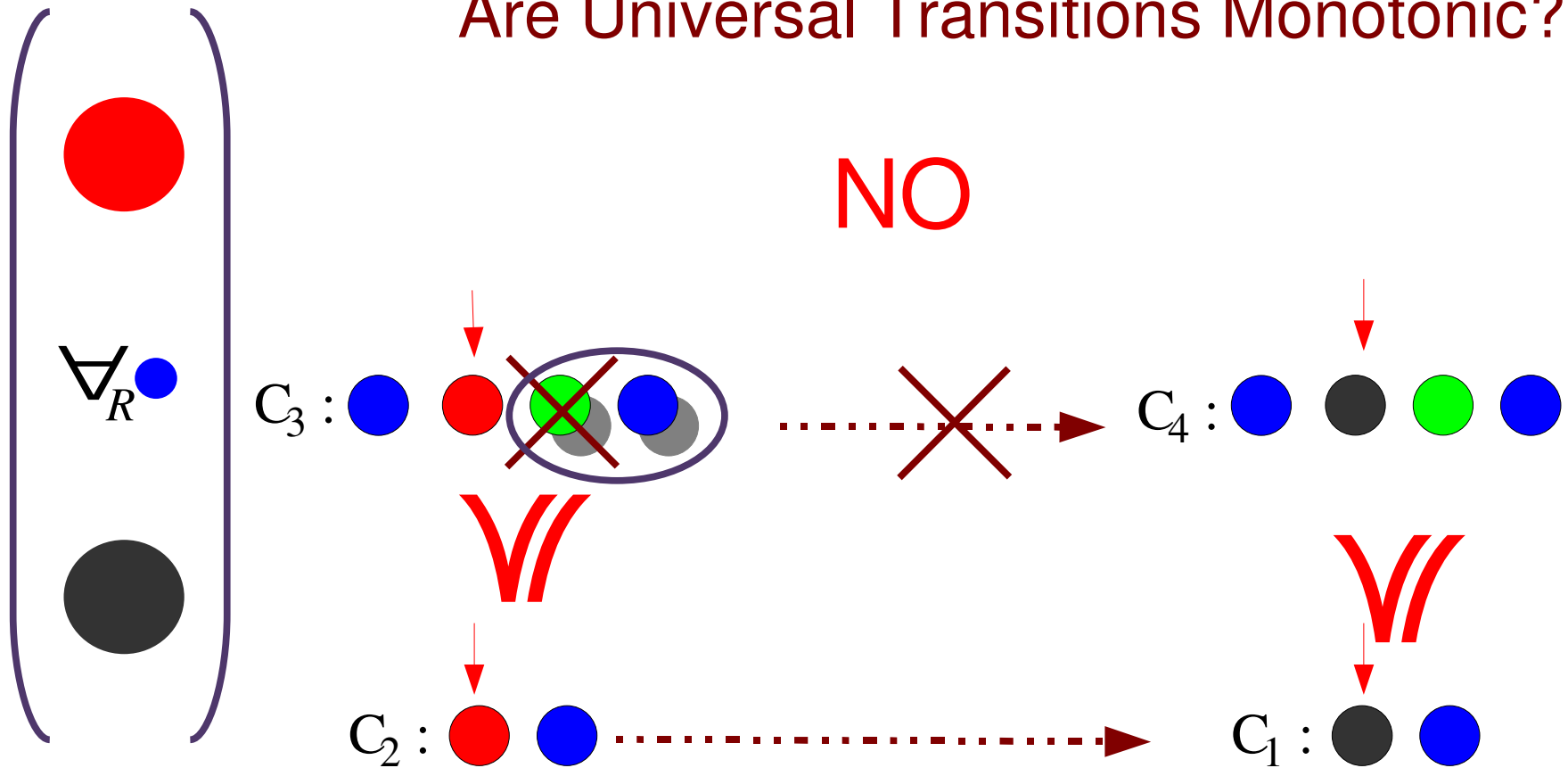
Are Universal Transitions Monotonic?



# Monotonicity

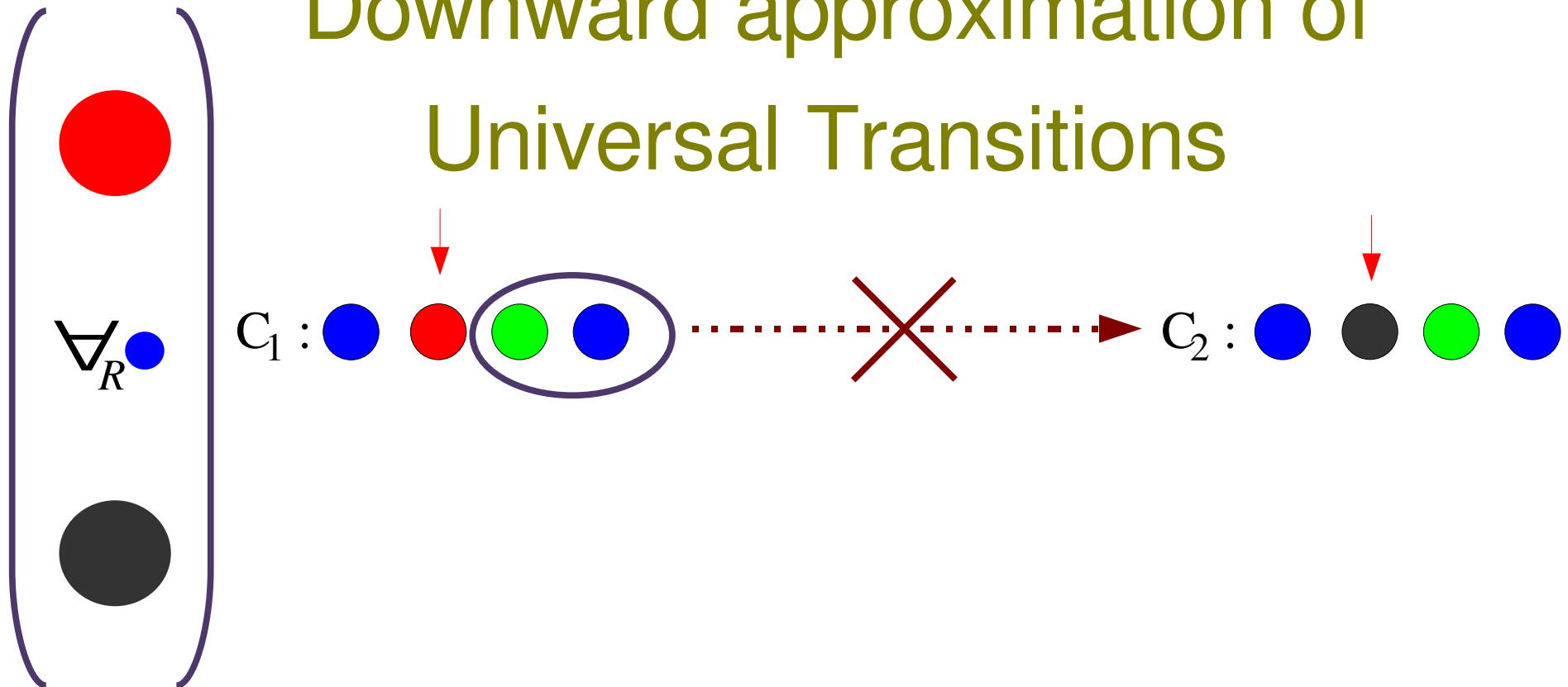
Are Universal Transitions Monotonic?

NO



# Approximation

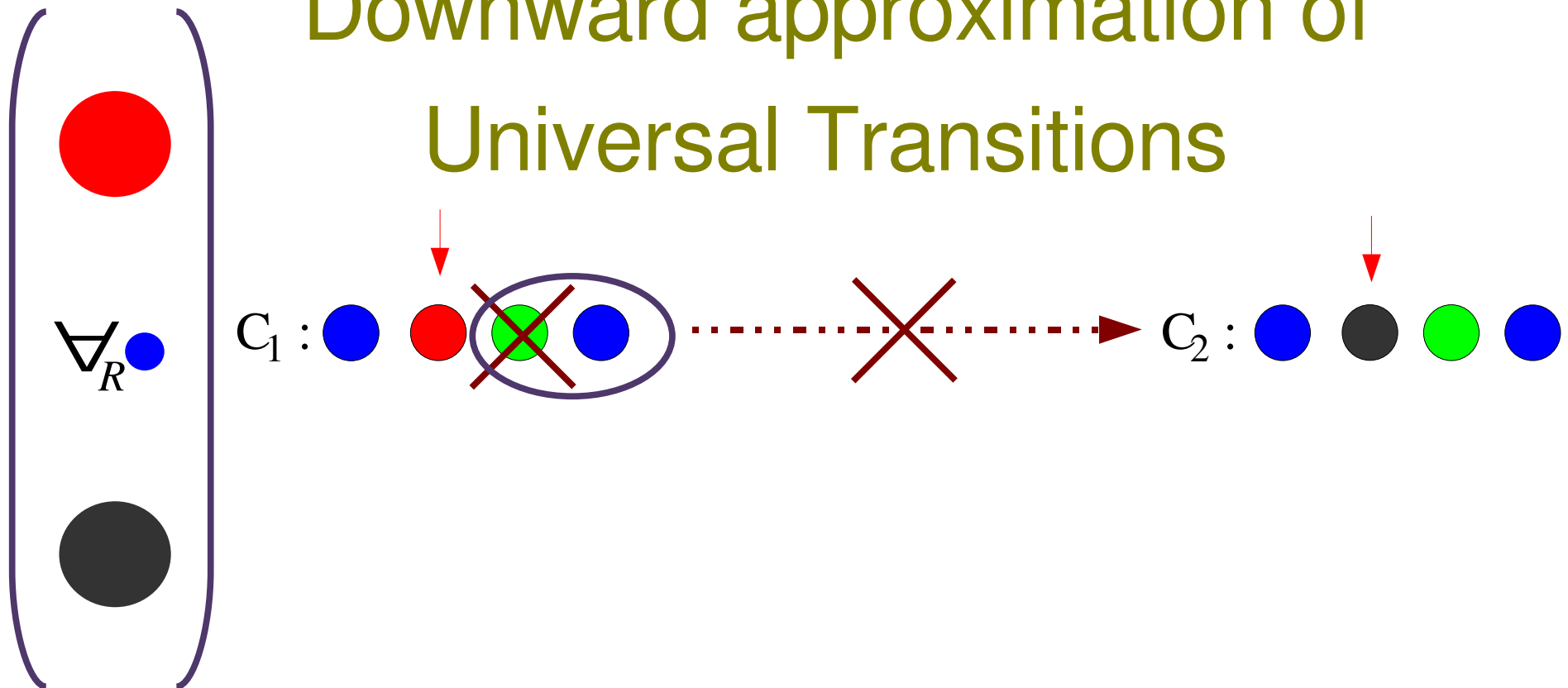
## Downward approximation of Universal Transitions





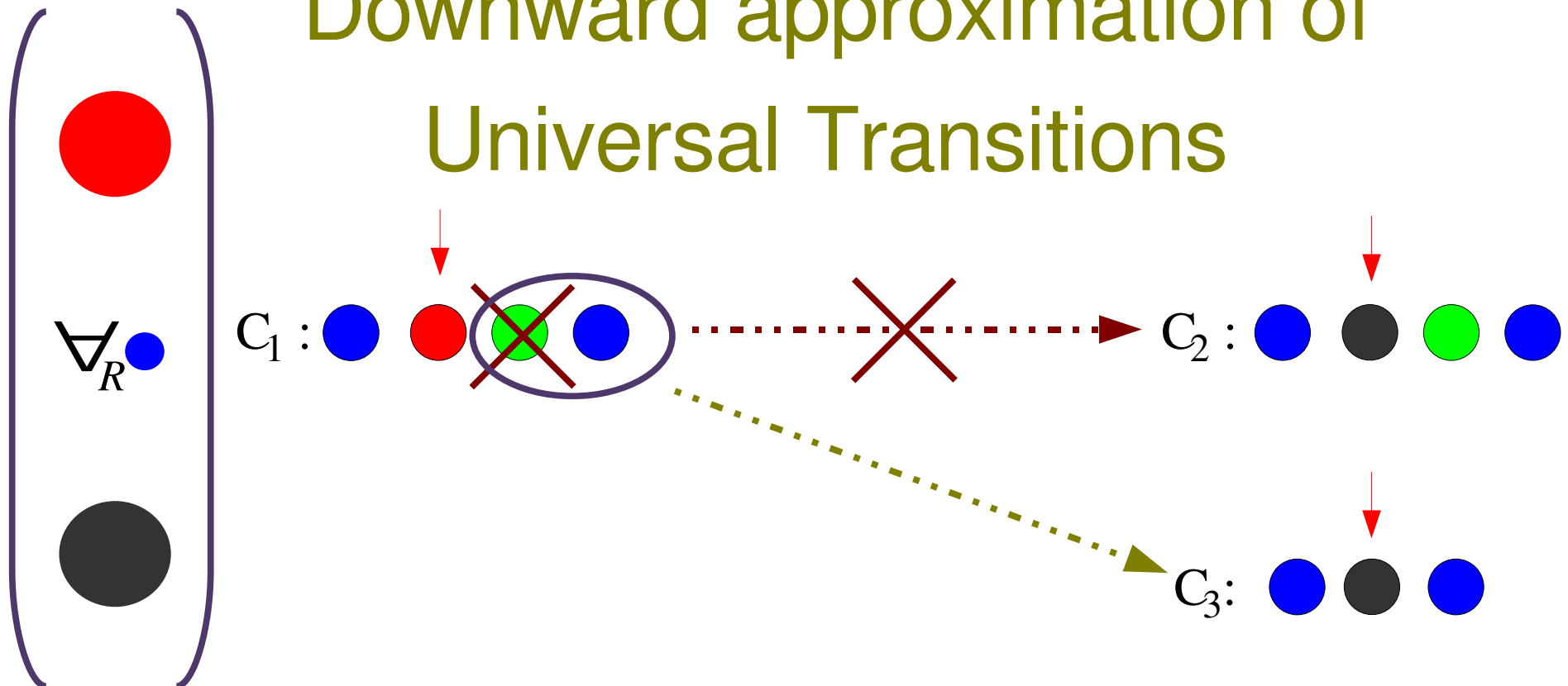
# Approximation

## Downward approximation of Universal Transitions



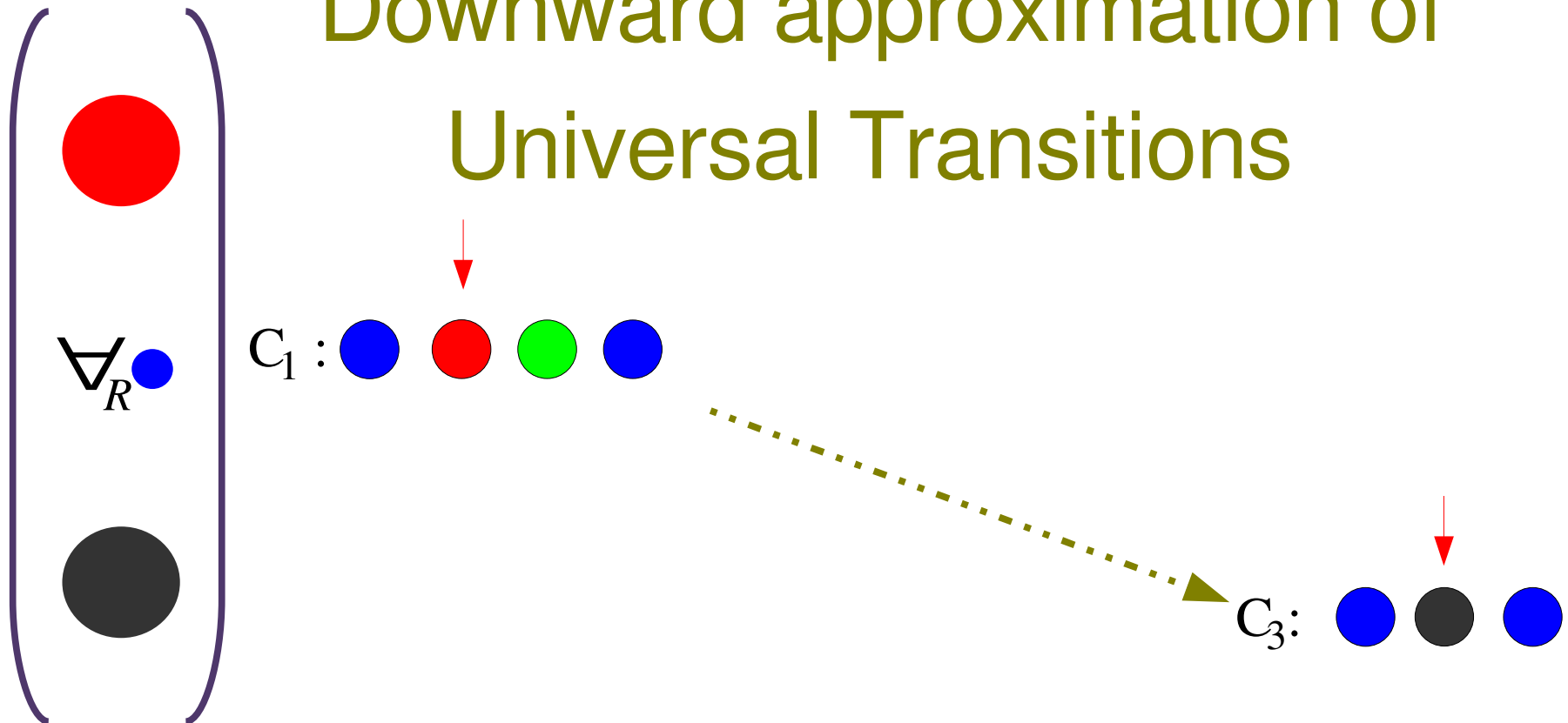
# Approximation

## Downward approximation of Universal Transitions



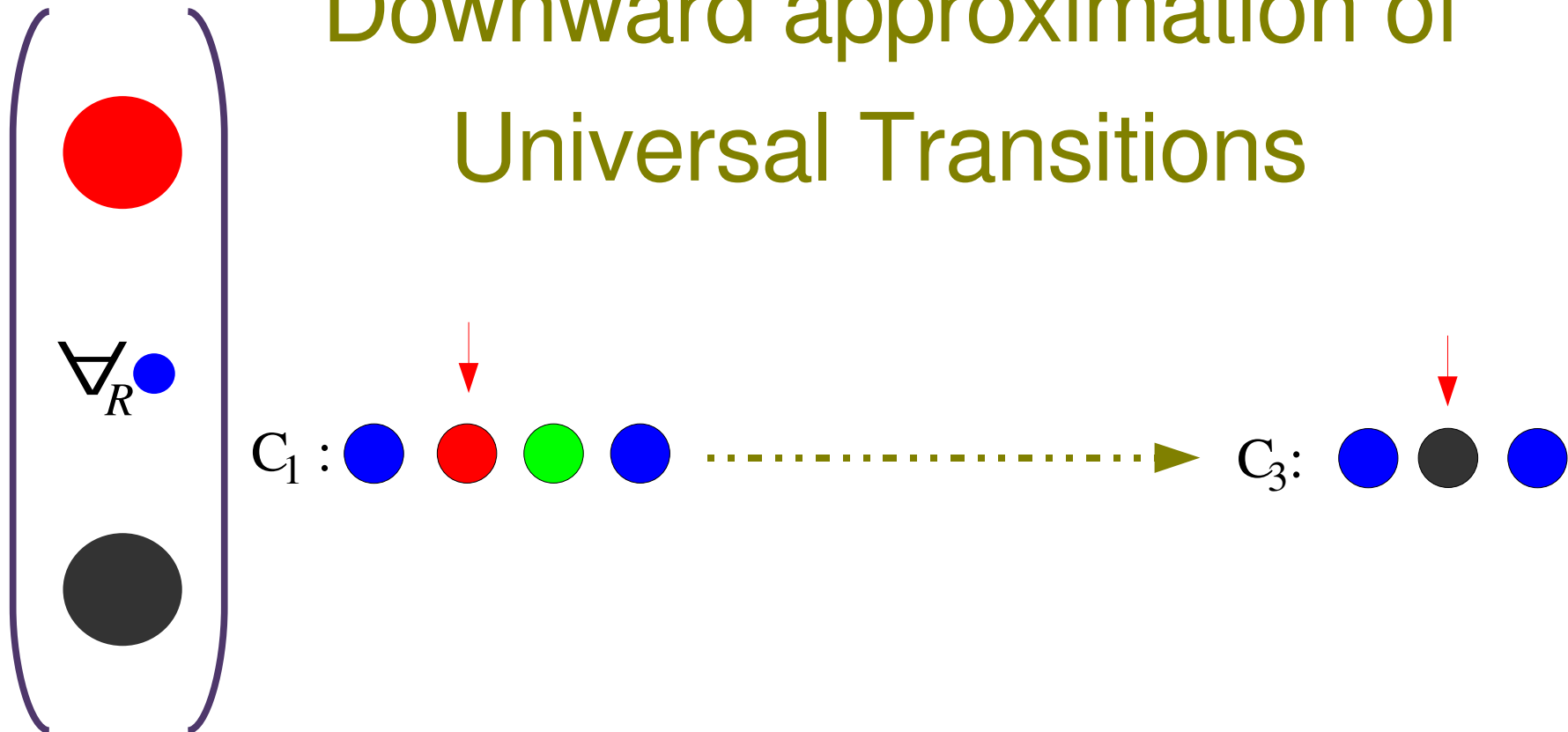
# Approximation

## Downward approximation of Universal Transitions



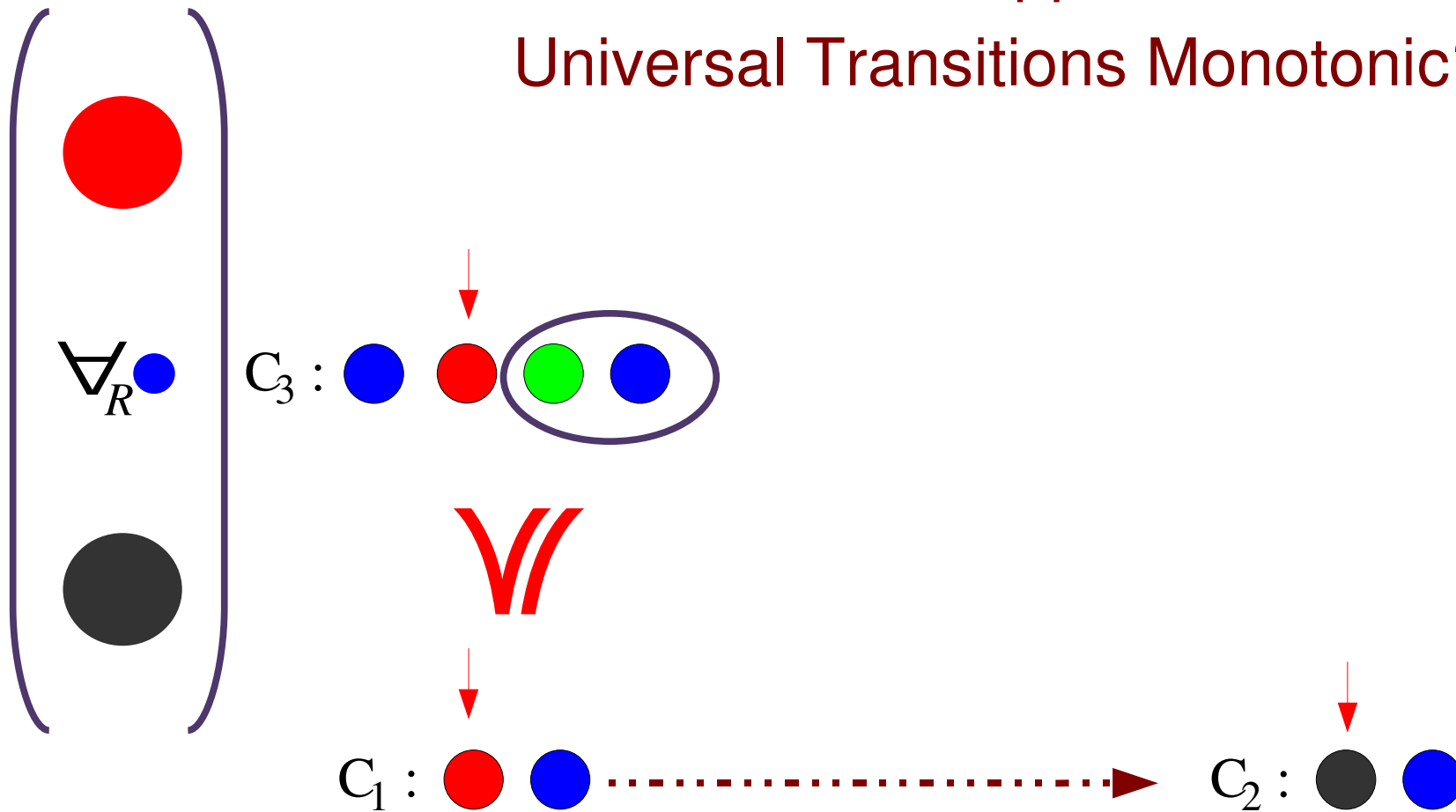
# Approximation

## Downward approximation of Universal Transitions



# Approximation

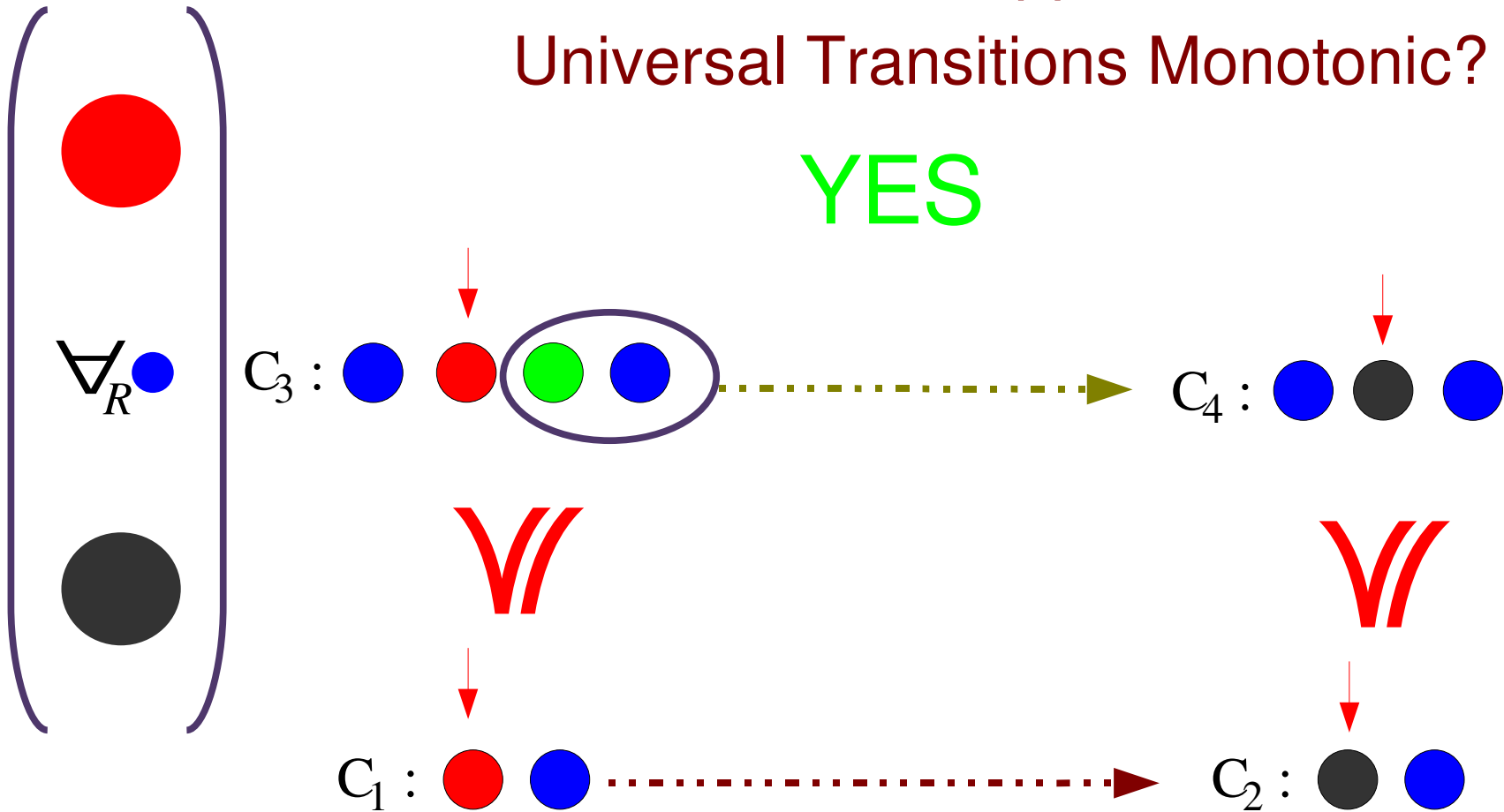
Are Downward Approximations of Universal Transitions Monotonic?



# Approximation

Are Downward Approximations of Universal Transitions Monotonic?

YES



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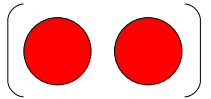
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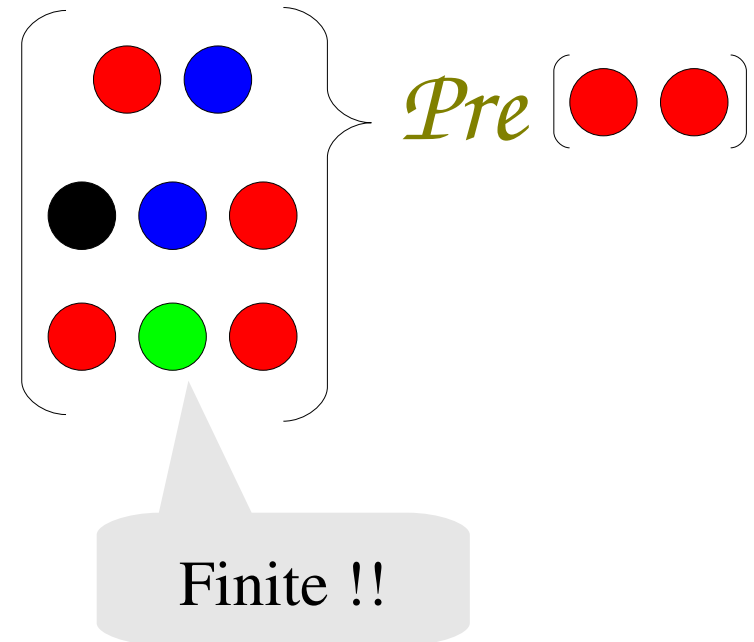
# Algorithm

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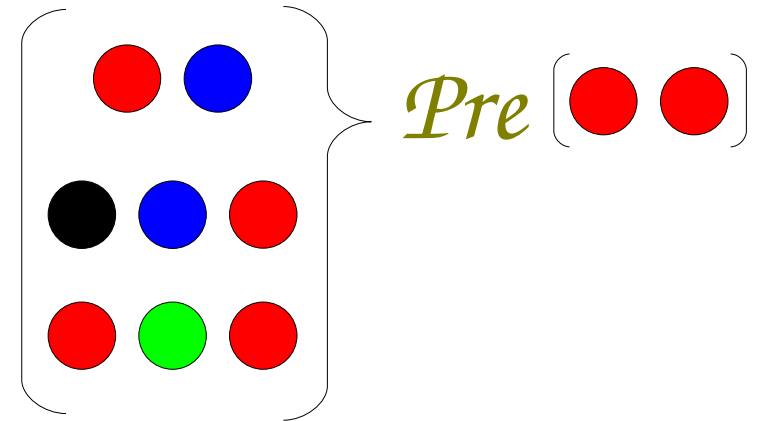
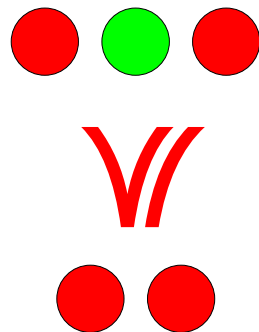
# Algorithm

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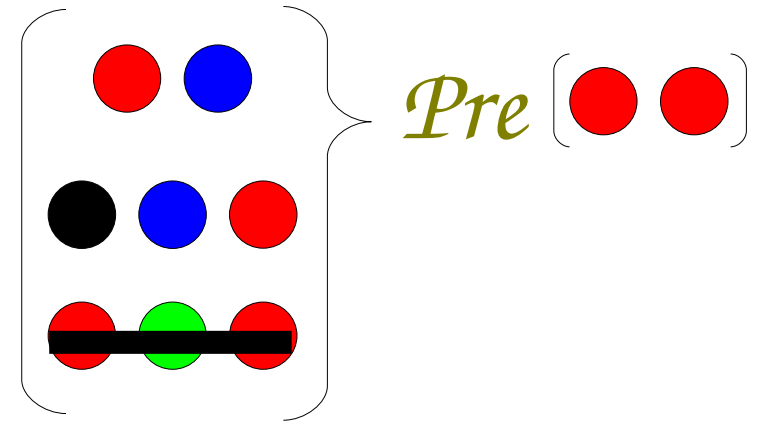
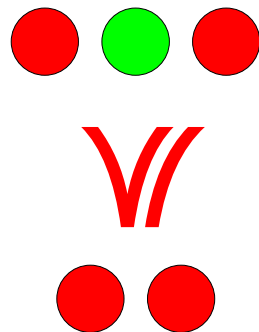
# Algorithm

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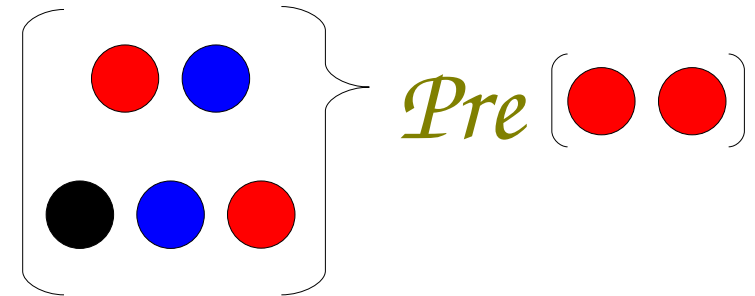
# Algorithm

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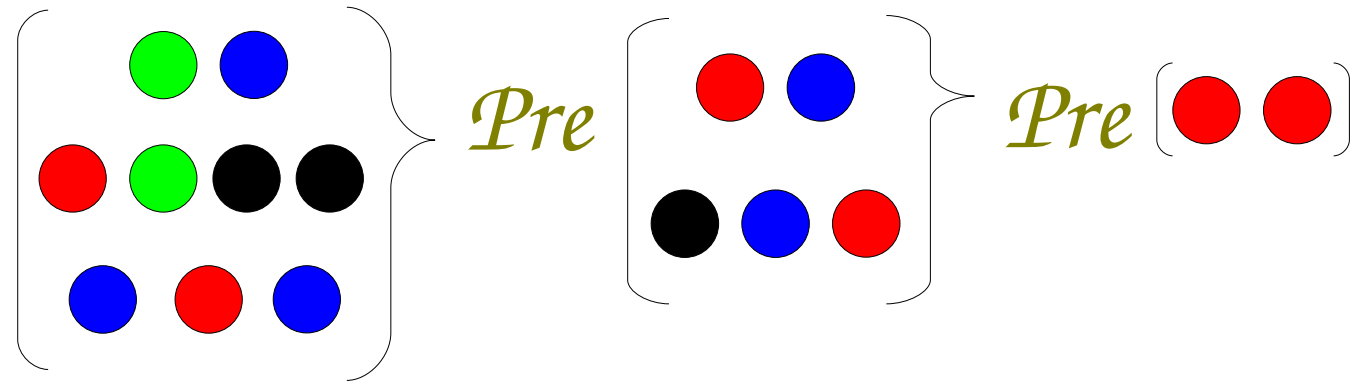
# Algorithm

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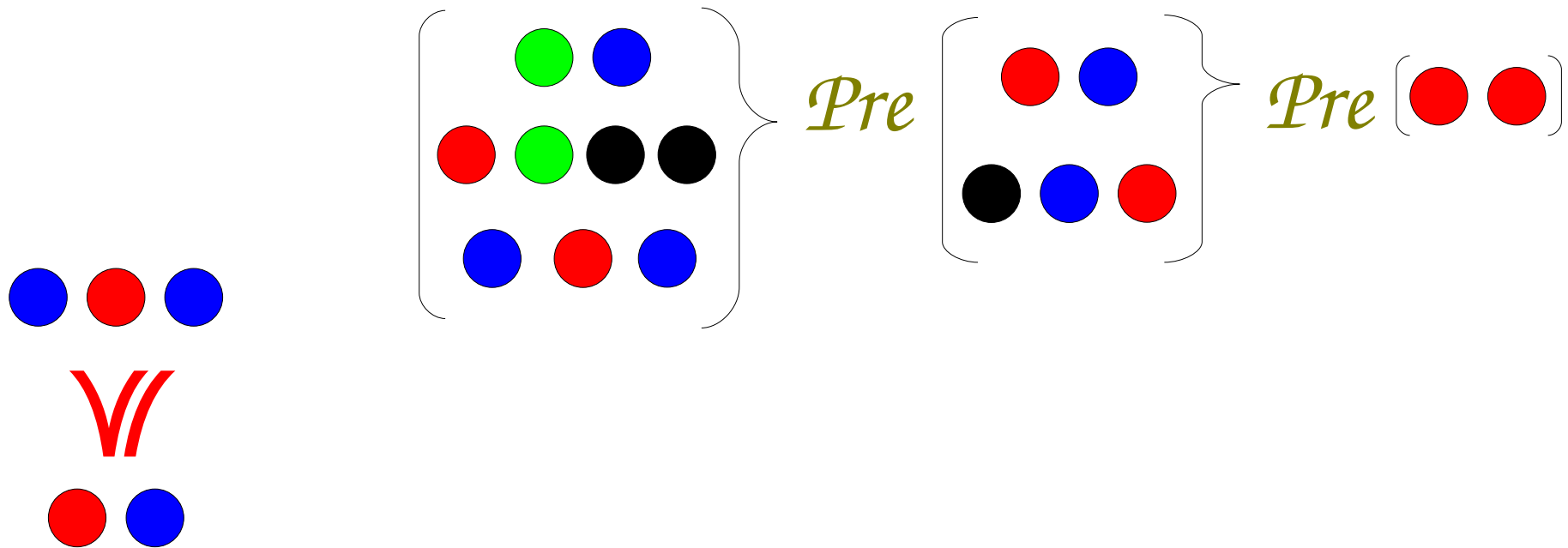


# Algorithm

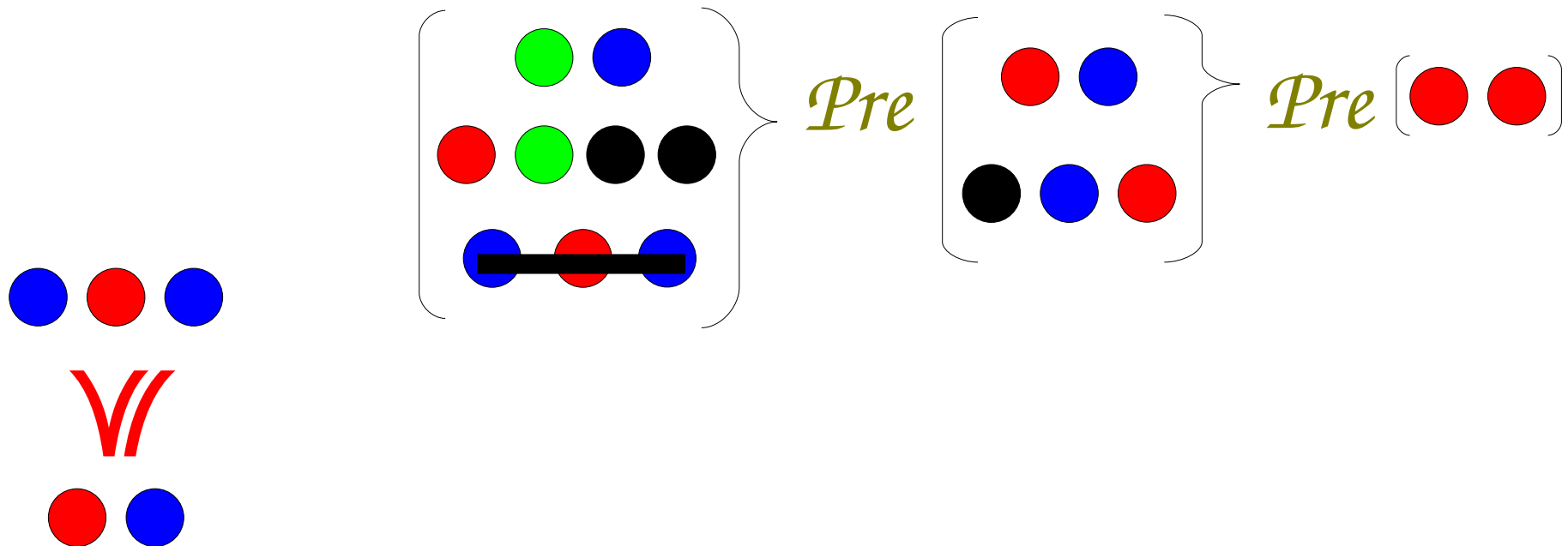
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# Algorithm



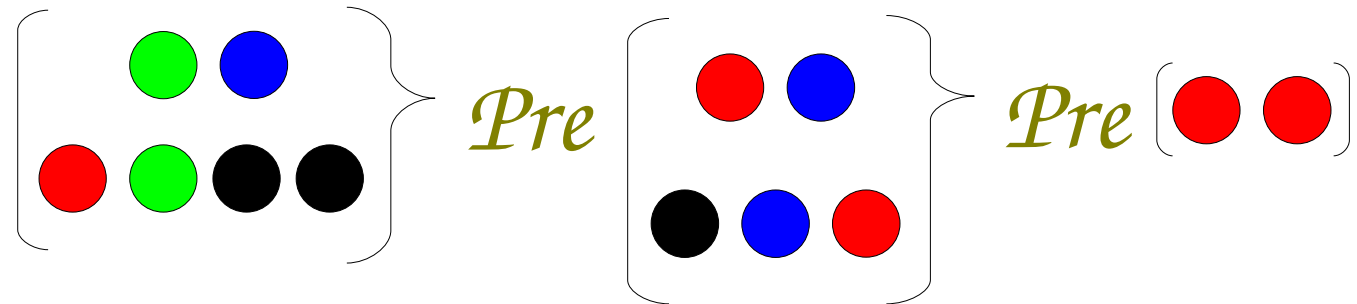
# Algorithm



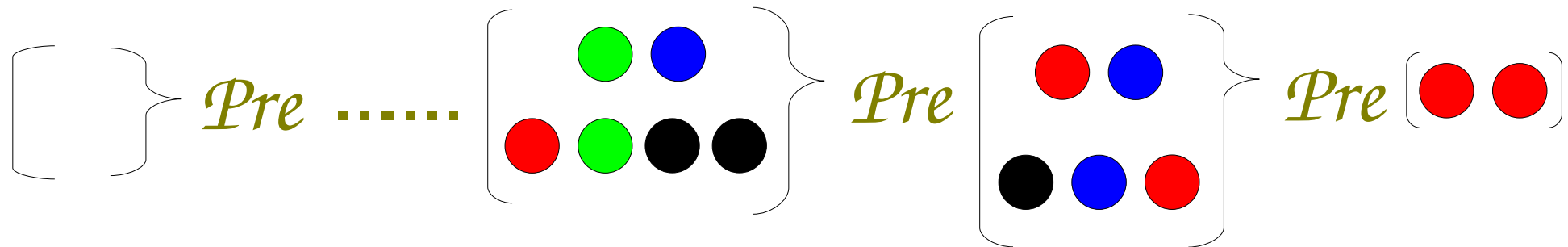


# Algorithm

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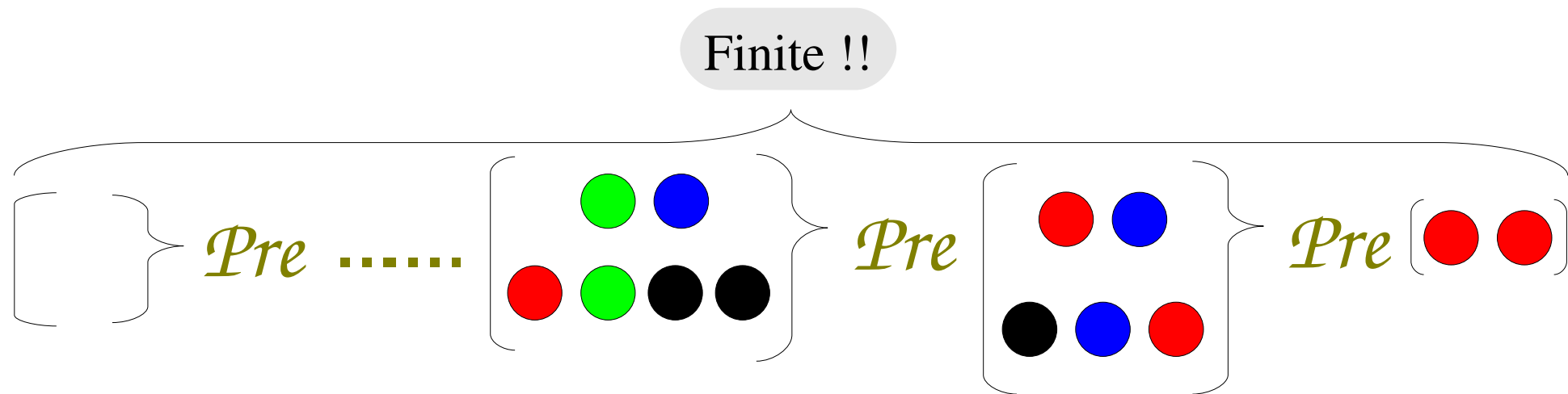
# Algorithm



Well Quasi Ordering:

“For each infinite sequence  $a_0, a_1, \dots$  there exists  $i < j$   
 such that  $a_i \preceq a_j$ ”

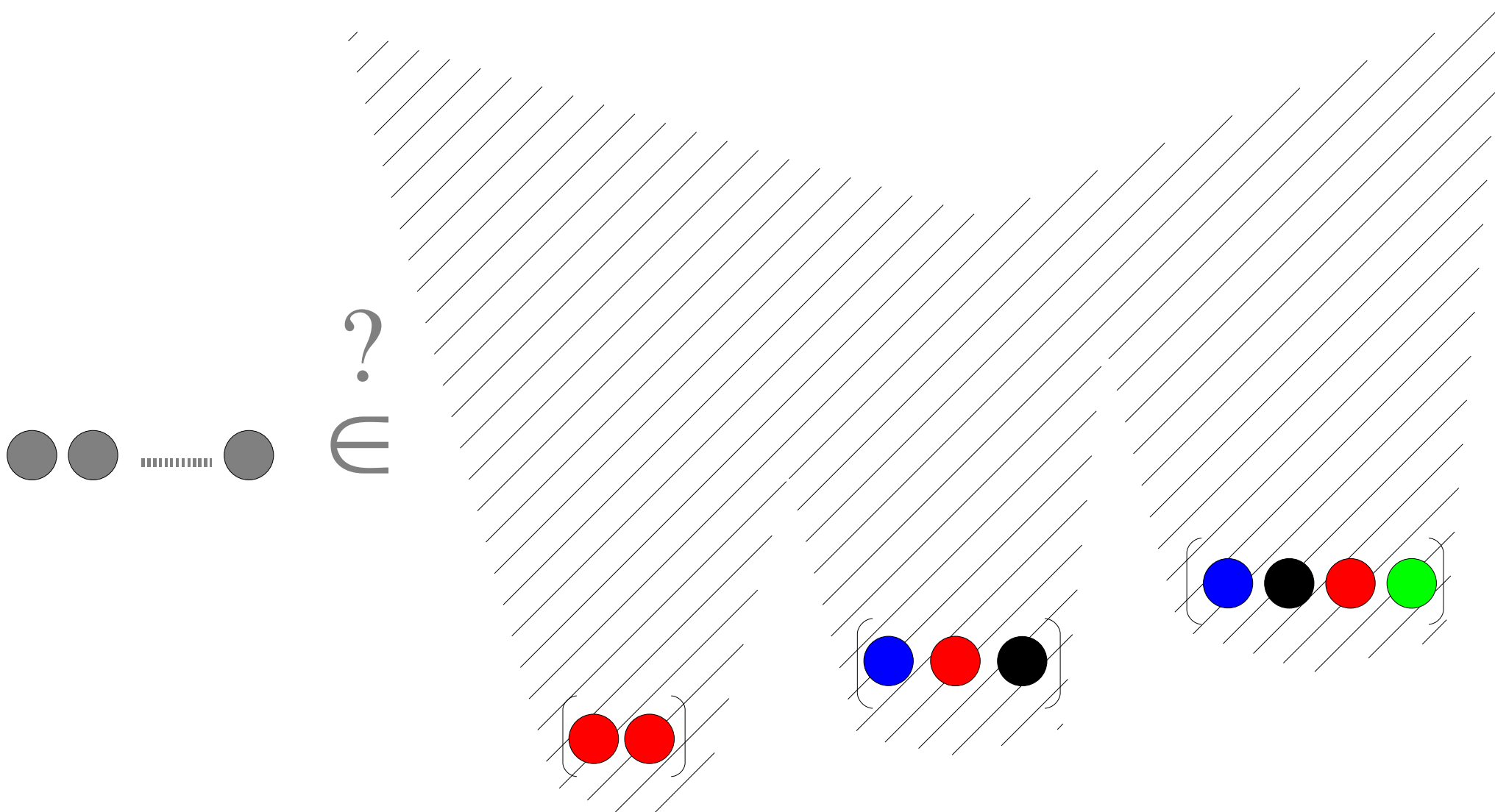
# Algorithm



Well Quasi Ordering:

“No infinite sequence of upward closed”

# Algorithm



# Results

	<i>#iter</i>	<i>#constr</i>	<i>T (ms)</i>
<i>Bakery</i>	2	2	4
<i>Bakery*</i>	2	2	4
<i>Burns</i>	14	71	230
<i>Burns*</i>	9	21	32
<i>Java M-lock</i>	5	24	30
<i>Java M-lock*</i>	5	17	30
<i>Dijkstra</i>	13	150	1700
<i>Dijkstra*</i>	8	57	168
<i>Szymanski</i>	17	334	3880
<i>Szymanski*</i>	17	334	4080

*Mutual Exclusion Algorithms*

	<i>#iter</i>	<i>#constr</i>	<i>t(ms)</i>
<i>Synapse</i>	3	3	4
<i>Berkley</i>	2	6	8
<i>Mesi</i>	3	8	8
<i>Moeisi</i>	1	12	12
<i>Dec Firefly</i>	3	11	16
<i>Xerox P.D</i>	3	20	52
<i>Illinois</i>	5	33	80
<i>Futurebus</i>	7	153	300
<i>German</i>	44	14475	3h45mn

*Cache Coherence Protocols*

# Conclusion

---

- A framework which can handle, e.g.
  - mutual exclusion and
  - cache coherence.
- Better performance than specialized tools
- Some of the examples are verified for the first time completely automatically (German, Java-Metalock)
- Can be extended to systems where the processes operate on unbounded variables (paper at CAV 2007)
- Simpler machinery compared to regular model checking (no transducers)
- Ongoing extensions to trees, graphs ...