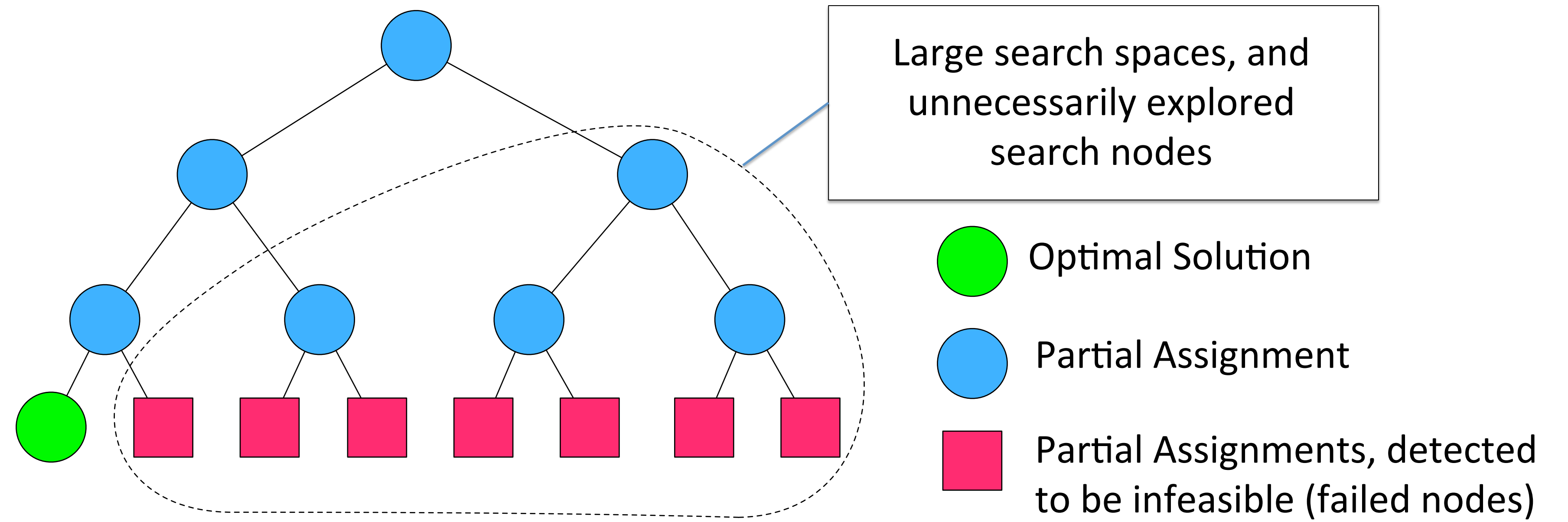


Generating Optimal Code

compiler
x combinatorial optimization
= **optimal code generation**

The Problem with Combinatorial Approaches: The Search Effort



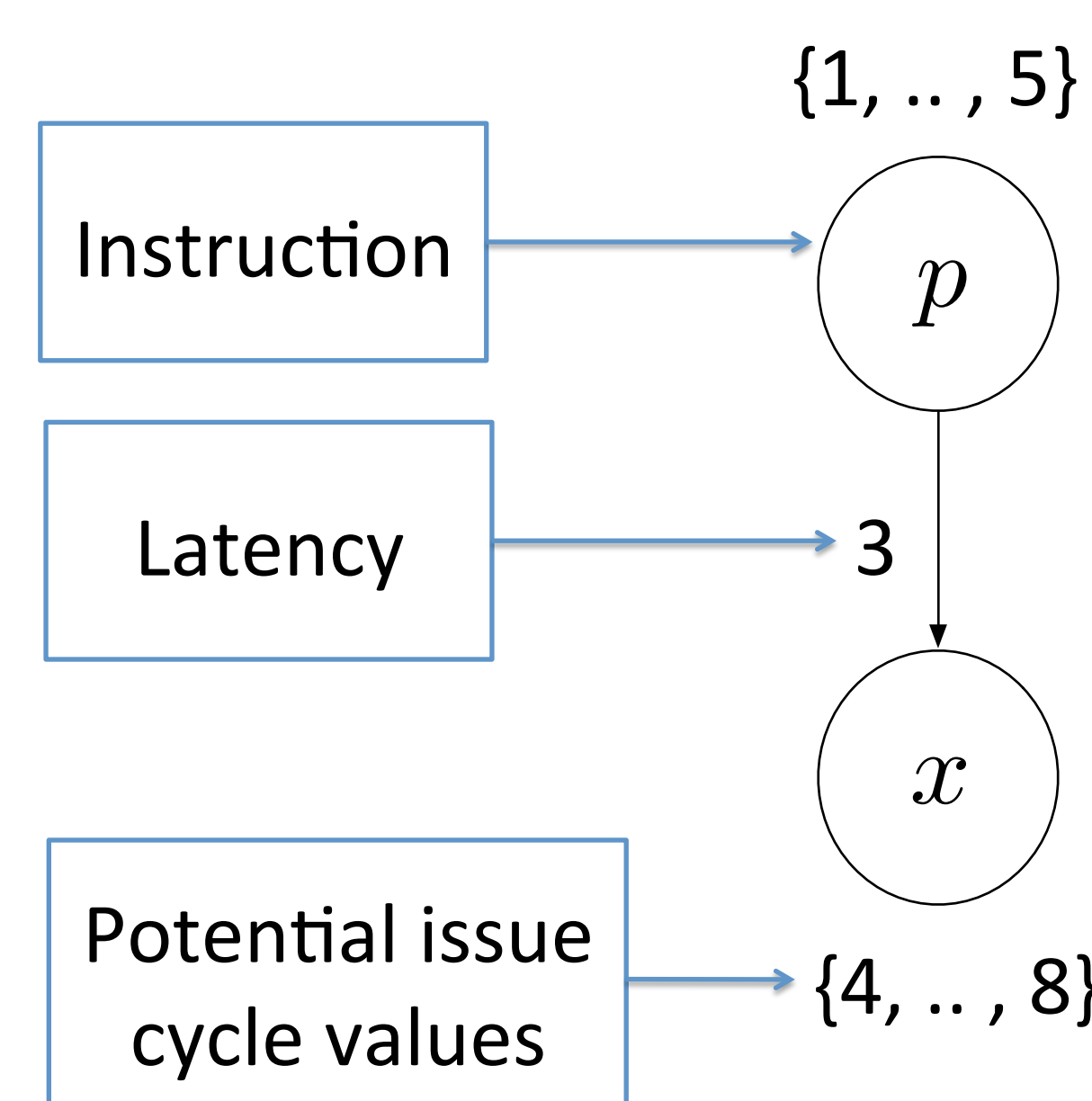
- Combinatorial approaches are often slower due to the large search effort
- For a constraint-based compiler, that would imply **long compilation times**

The Key to Speeding Up Solution Search

- The Unison project [1] uses Constraint Programming (CP), a combinatorial optimization approach, to implement a constraint-based compiler
- In CP, a problem is modeled with variables and relations among these variables (that is, constraints)
- A constraint may be a base constraint (modeling core problem), or an implied constraint (modeling logically redundant relations)

Implied constraints may provide a different point-of-view on the problem, that may help to **skip exploring infeasible assignments at an early stage** of search

Base Constraints for Instruction Scheduling



Precedence Constraint

An instruction x may not start execution before its predecessor p was issued and its latency has passed:

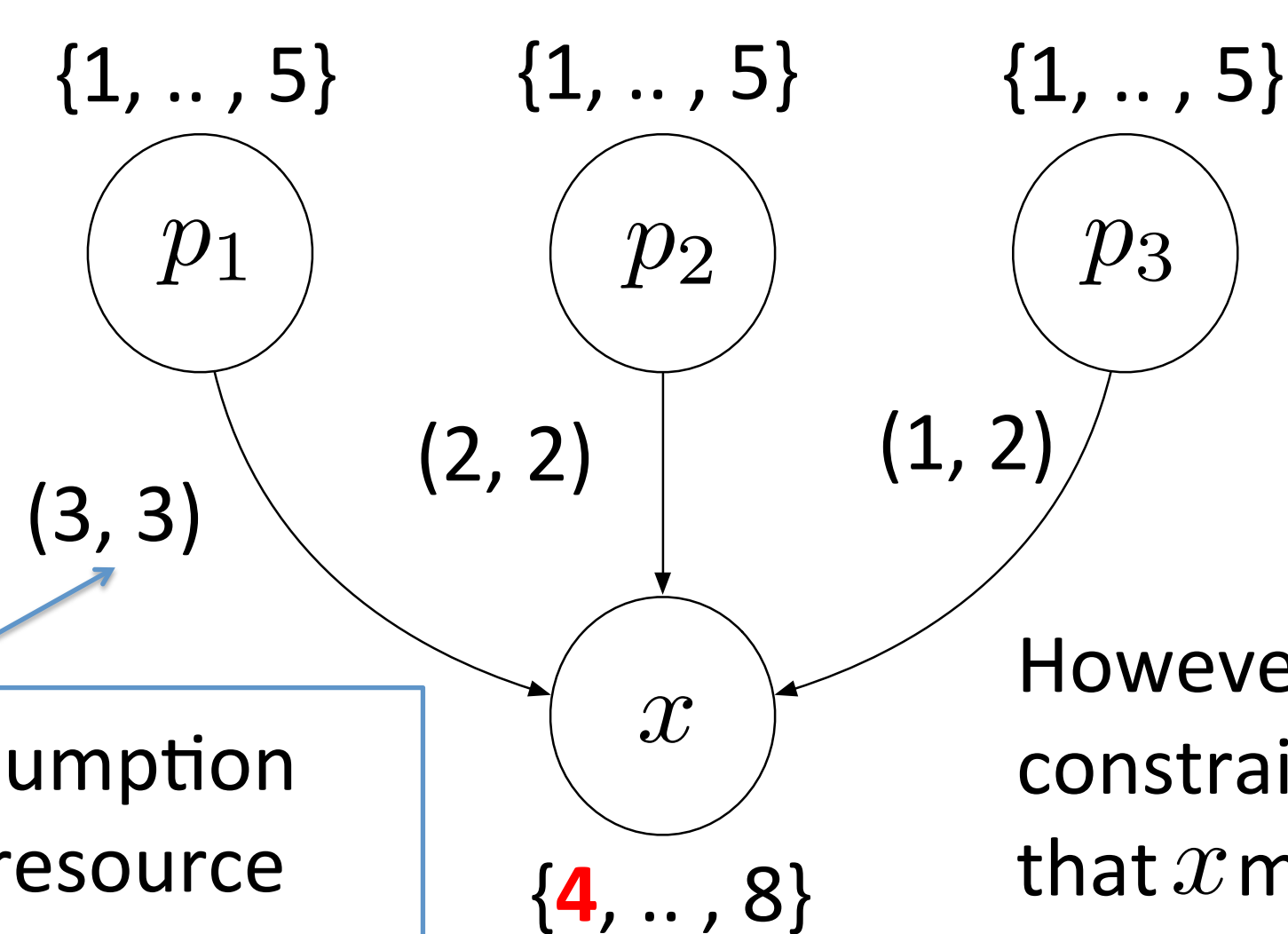
$$c_x \geq c_p + \text{lat}(p)$$

with c_* denoting the issue cycle
 $\text{lat}(*)$ denoting the latency

The precedence constraint holds for the example on the left.

Looking at the bigger picture

Insight: If we take several predecessors into consideration, we find out that x can never start at issue cycle 4: all of its predecessors consume the same unique resource.



However, the precedence constraints do not detect that x may not start at issue cycle 4!

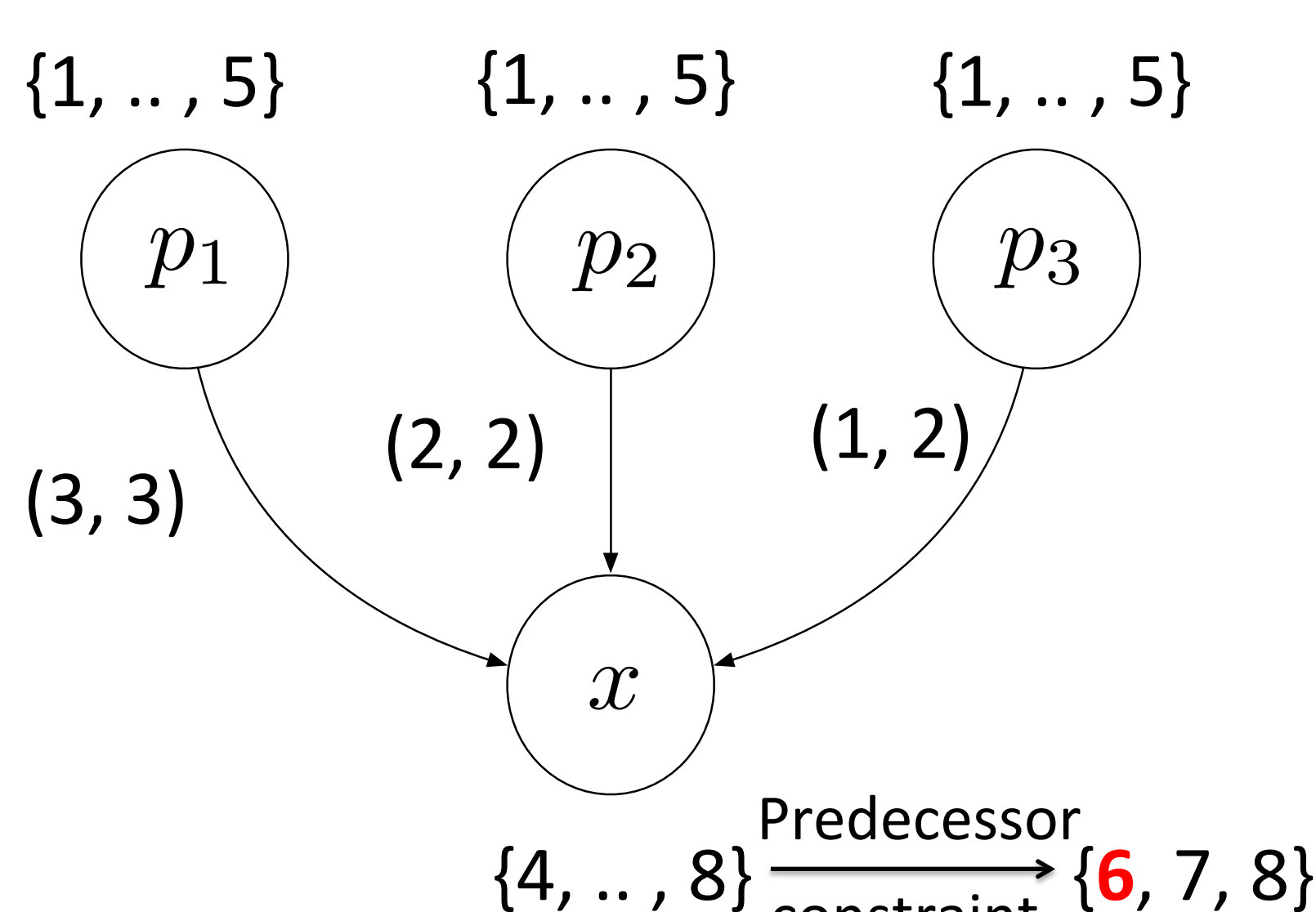
An implied constraint: The Predecessor Constraint

For each instruction i , its predecessor set P and a resource r , add a **predecessor constraint** (extended from [2]):

$$\text{lower}(c_i) \geq \min\{\text{lower}(c_p) \mid p \in P\} + \left\lceil \frac{\sum_{p \in P} \text{dur}(p, r) * \text{con}(p, r)}{\text{cap}(r)} \right\rceil - \max\{\text{dur}(p, r) \mid p \in P\} + \min\{\text{lat}(p) \mid p \in P\}$$

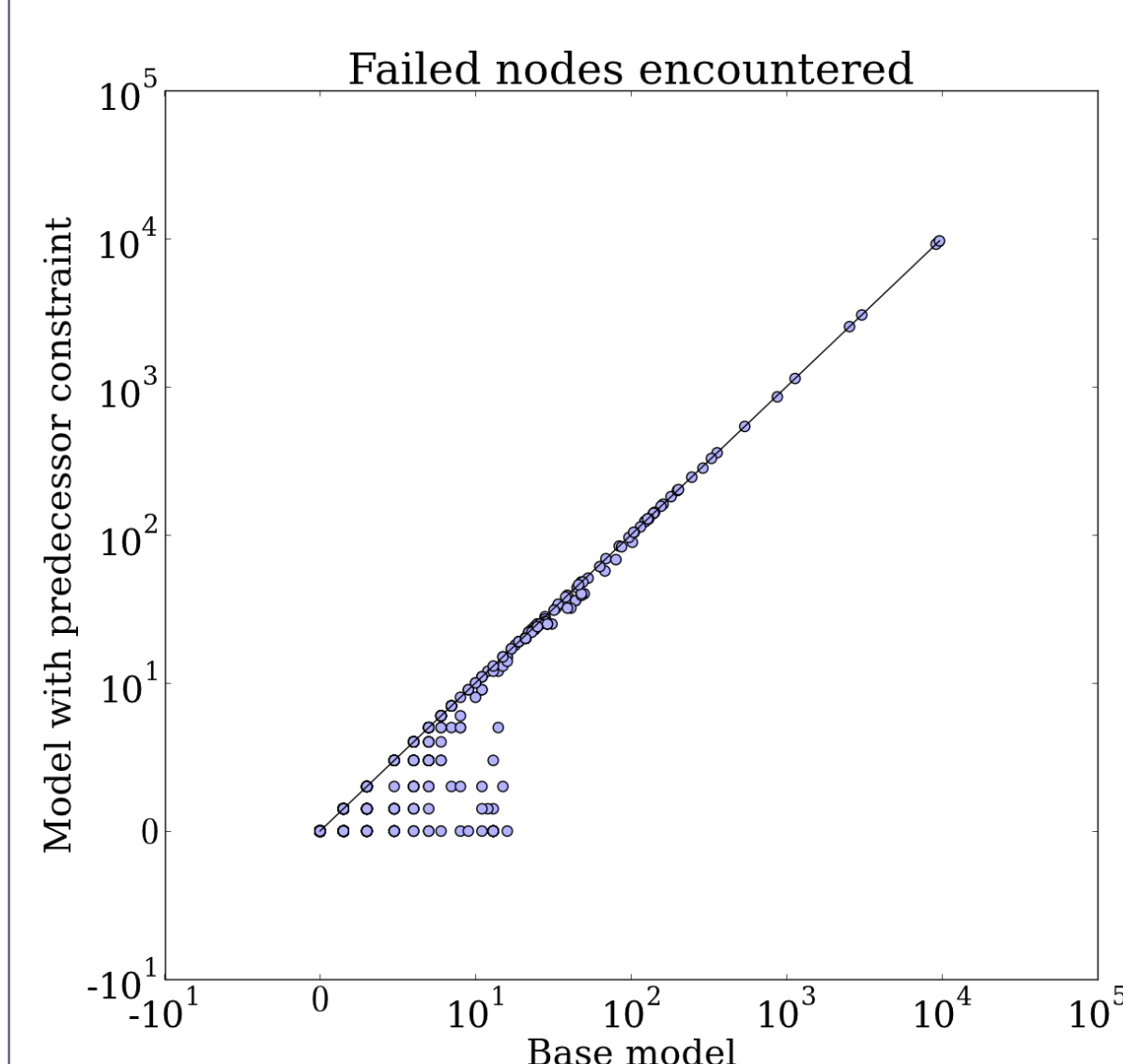
with $\text{cap}(r)$ being the capacity of resource r
 $\text{con}(p, r)$ denoting how many units of r are consumed by p
 $\text{dur}(p, r)$ denoting the number of cycles in which p consumes r
 $\text{lower}(*)$ being the lower bound of a domain

Applying the Constraint



Assuming $\text{cap}(r) = \text{con}(p_*, r) = 1$

Impact of Predecessor Constraints on bzip2



- Figure shows encountered failed nodes for base and extended model during solution search for a basic block
- Extended model with predecessor constraints significantly **cuts down the number of failed nodes** (in total for 291 basic blocks)
- Achieves **to find optimal solutions for four more basic blocks** within a time limit of 30 seconds

References

- [1] R. Castañeda Lozano, M. Carlsson, G. Hjort Blindell, and C. Schulte. Combinatorial spill code optimization and ultimate coalescing. In Proc. of LCTES'14
- [2] A. M. Malik, J. McInnes, and P. van Beek. Optimal basic block instruction scheduling for multiple-issue processors using constraint programming. In International Journal on Artificial Intelligence Tools 2008