

# Modeling and Analysis of Data Flow Graphs using the Digraph Real-Time Task Model

Morteza Mohaqeqi, Jakaria Abdullah, and Wang Yi

Uppsala University

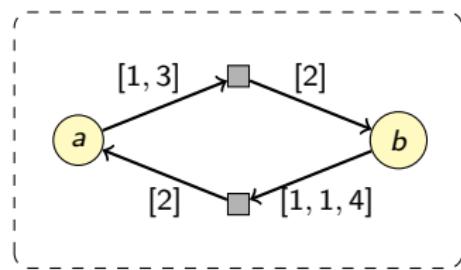
Ada-Europe 2016



# Introduction

Data Flow Graphs:

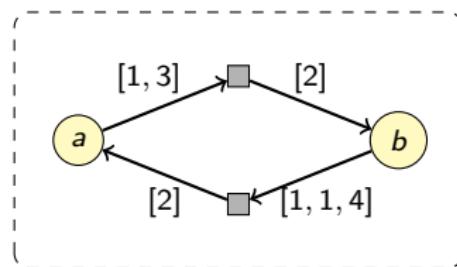
- Signal processing
- Stream processing
- Data dependency



# Introduction

Data Flow Graphs:

- Signal processing
- Stream processing
- Data dependency



## Design Objectives

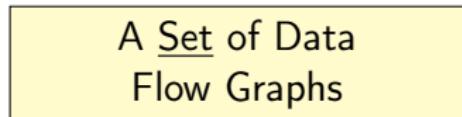
Throughput maximization

## Design Constraints

- Buffer overflow/underflow avoidance
- Schedulability

# An Overview

- The Problem:



Schedule

- Our Approach:



Transform

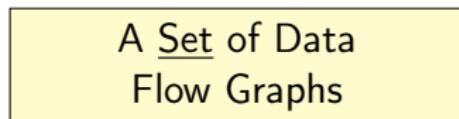
Real-Time Tasks

Schedule

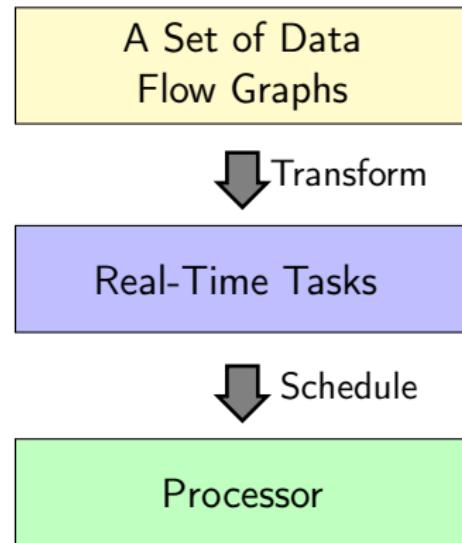
Processor

# An Overview

- The Problem:

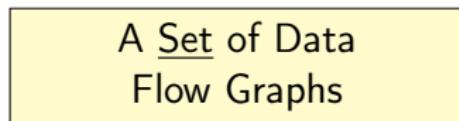


- Our Approach:

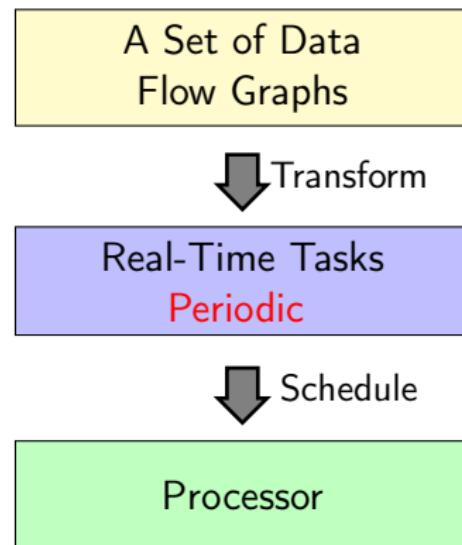


# An Overview

- The Problem:

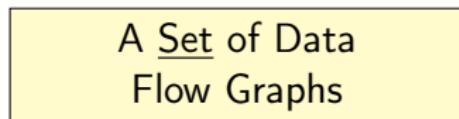


- Our Approach:

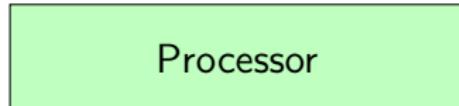


# An Overview

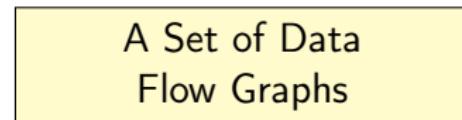
- The Problem:



Schedule



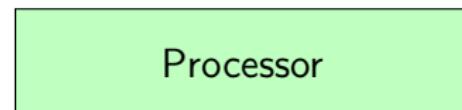
- Our Approach:



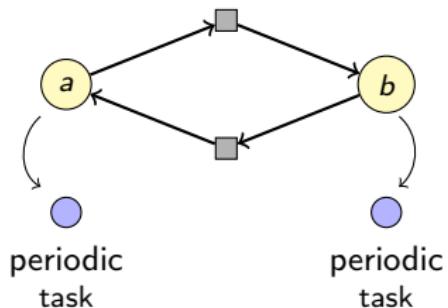
Transform



Schedule



# Previous Work

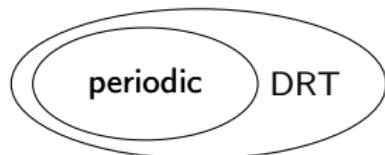
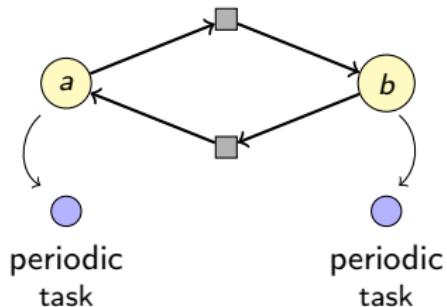


Our work

Strictly Period Schedule  
[Bouakaz 2014]

Digraph Real-Time (DRT)  
task model [Stigge et al 2013]

# Previous Work



Our work

Strictly Period Schedule  
[Bouakaz 2014]

Digraph Real-Time (DRT)  
task model [Stigge et al 2013]

# Outline

1 Introduction

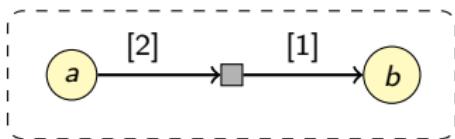
2 Method

3 Evaluation

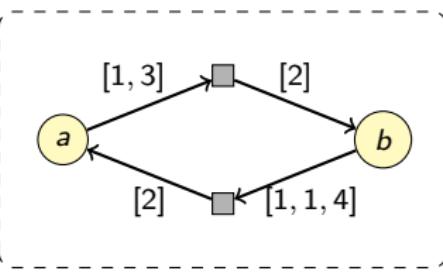
4 Conclusion

# (Static) Data Flow Graphs

## Synchronous Data Flow



## Cyclo-Static Data Flow

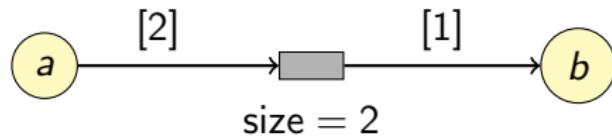


- Fixed token production (consumption) rate
- Fixed execution time

- **Variable** token production (consumption) rate
- **Variable** execution time

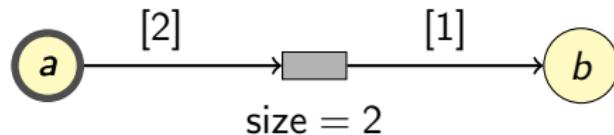
# Semantics

- Empty buffer



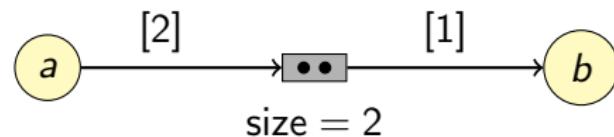
# Semantics

- Empty buffer
- 'a' can be fired



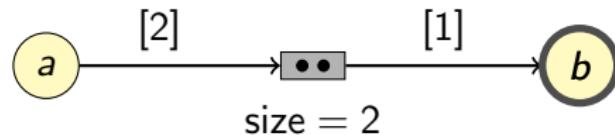
# Semantics

- Full buffer



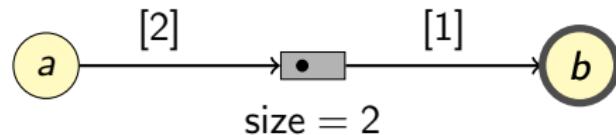
# Semantics

- Full buffer
- '**a**' **cannot** be fired
- '**b**' **can** be fired



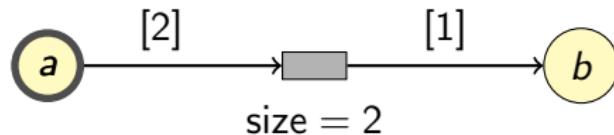
# Semantics

- '**a**' **cannot** be fired
- '**b**' **can** be fired



# Semantics

- Empty buffer
- 'a' can be fired



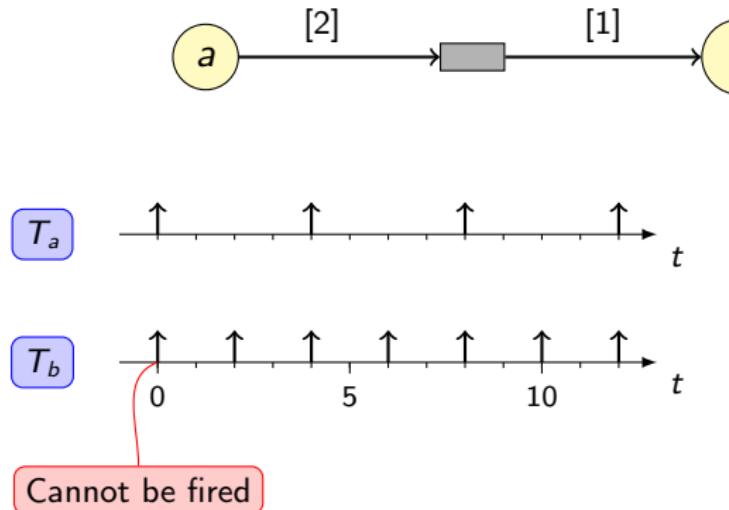
# Constraints

## Design Constraints

- Underflow/overflow avoidance
- Schedulability

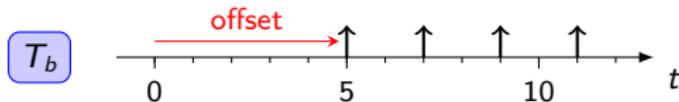
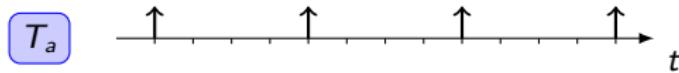
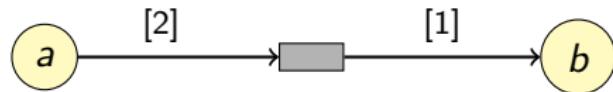
# Underflow and Overflow

- Underflow avoidance



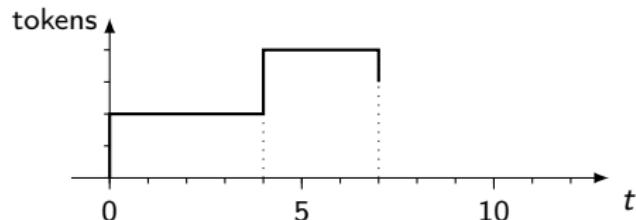
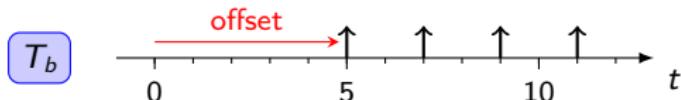
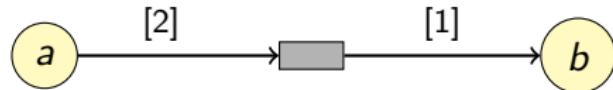
# Underflow and Overflow

- Underflow avoidance



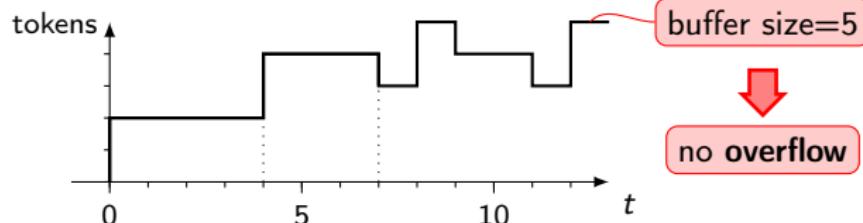
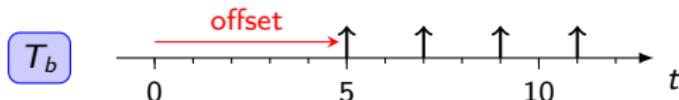
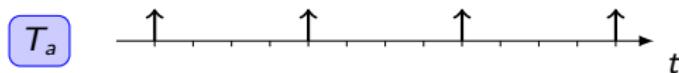
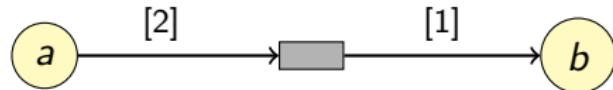
# Underflow and Overflow

- Produce token as **soon** as possible
- Consume token as **late** as possible



# Underflow and Overflow

- Produce token as **soon** as possible
- Consume token as **late** as possible



# Constraints

## Design Constraints

- Underflow/overflow avoidance

# Constraints

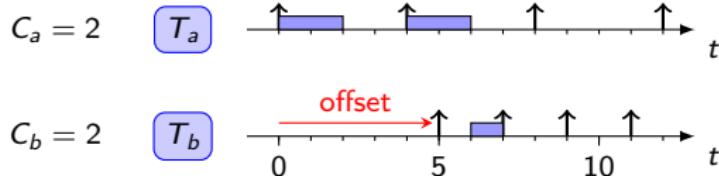
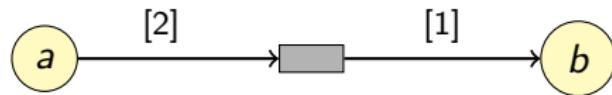
## Design Constraints

- Underflow/overflow avoidance
- Schedulability

# Constraints

## Design Constraints

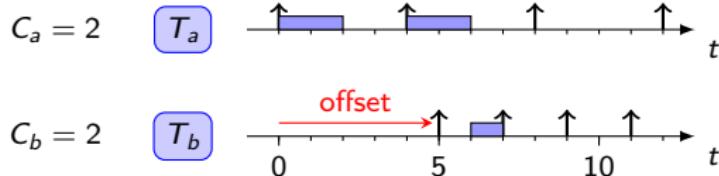
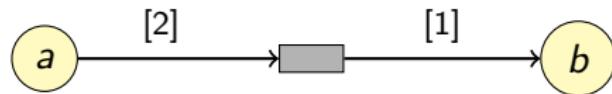
- Underflow/overflow avoidance
- Schedulability



# Constraints

## Design Constraints

- Underflow/overflow avoidance
- Schedulability

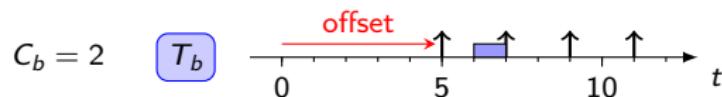
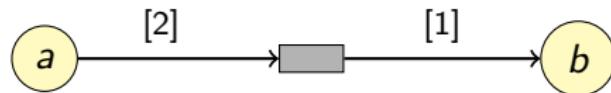


Unschedulable!

# Constraints

## Design Constraints

- Underflow/overflow avoidance
- Schedulability



Larger Periods

Lower Throughput

# The Problem

## Design Parameters

- Periods
- Offsets

## Constraints

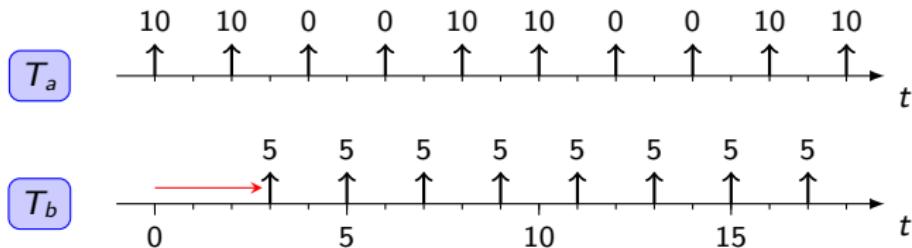
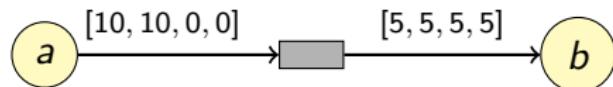
- No underflow
- No overflow
- Schedulability

## Objective

Throughput maximization

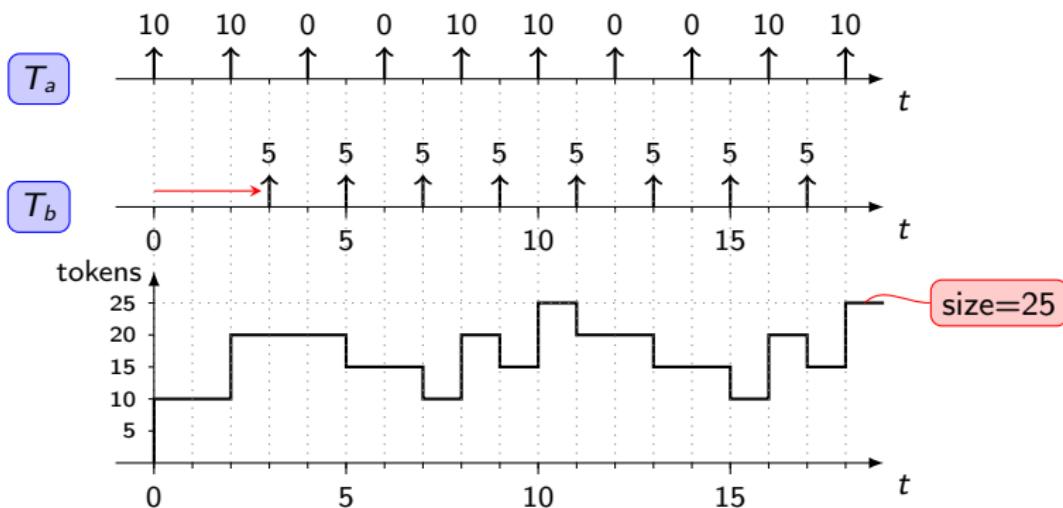
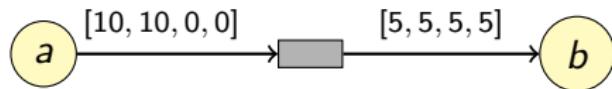
# Cyclo-Static Data Flow Graphs

- Repeating pattern



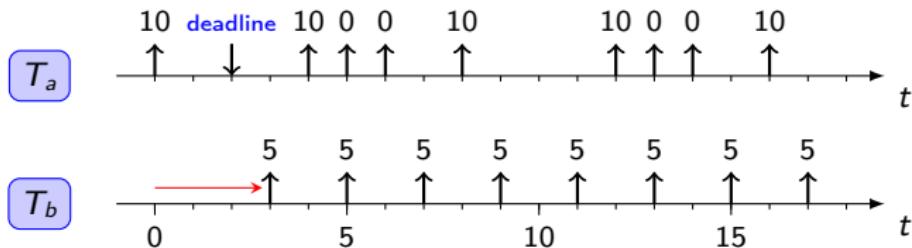
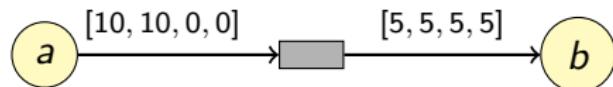
# Cyclo-Static Data Flow Graphs

- Repeating pattern



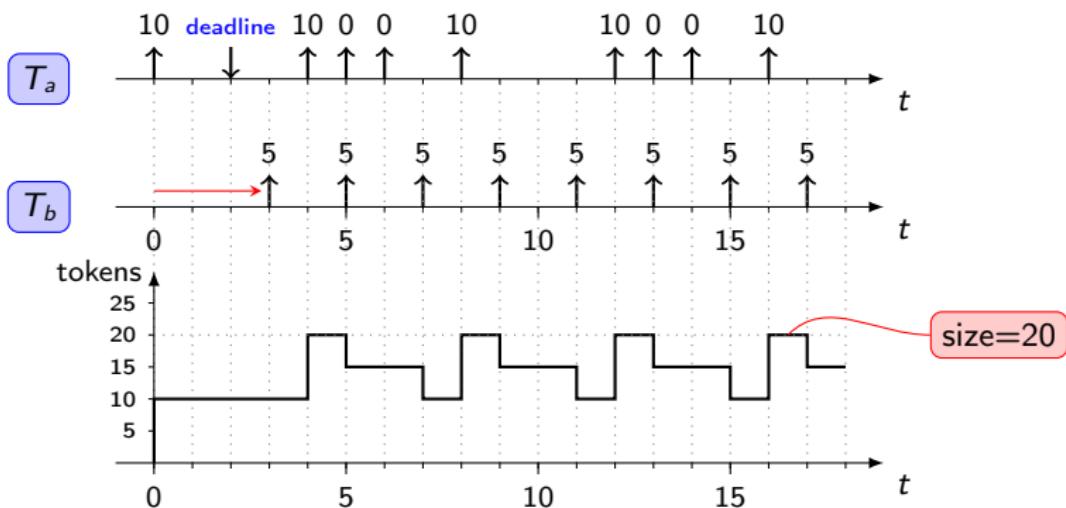
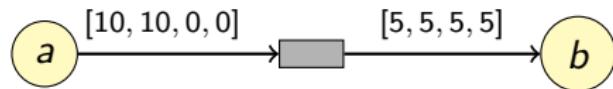
## Cyclo-Static Data Flow Graphs

- Repeating pattern



# Cyclo-Static Data Flow Graphs

- Repeating pattern

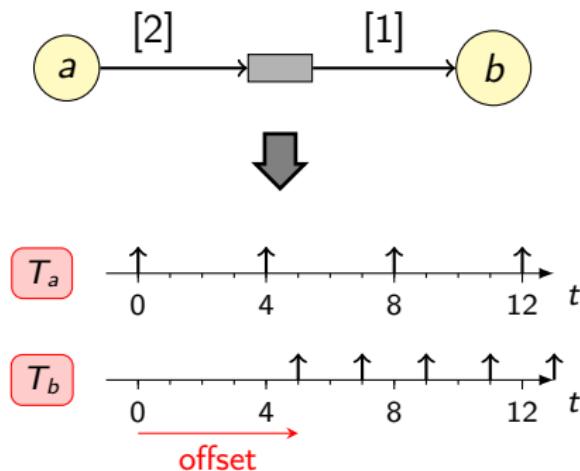


We need a **non-periodic** task model

# Scheduling Data Flow Graphs

## Synchronous Data Flow

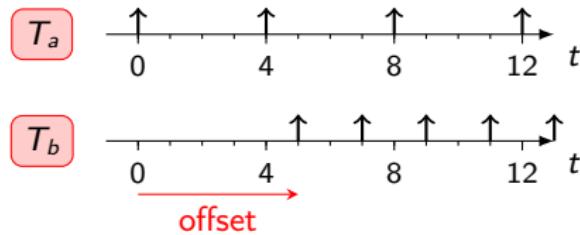
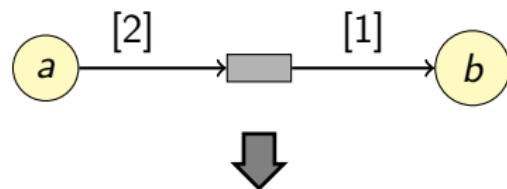
- Fixed behavior
- Periodically repeating



# Scheduling Data Flow Graphs

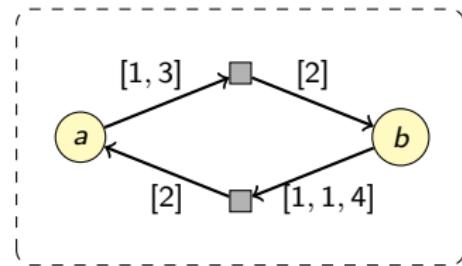
## Synchronous Data Flow

- Fixed behavior
- Periodically repeating



## Cyclo-Static Data Flow

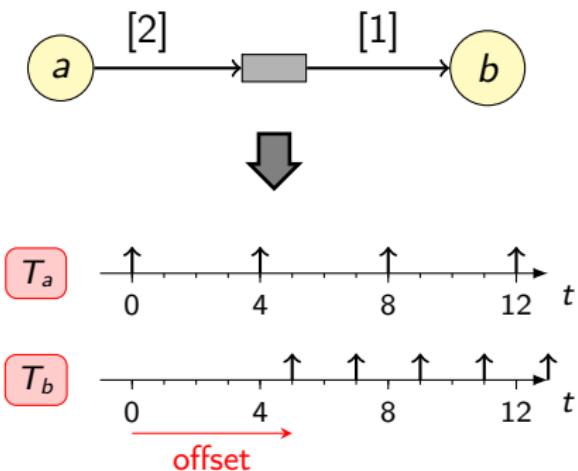
- Changing behavior
- Repeating pattern



# Scheduling Data Flow Graphs

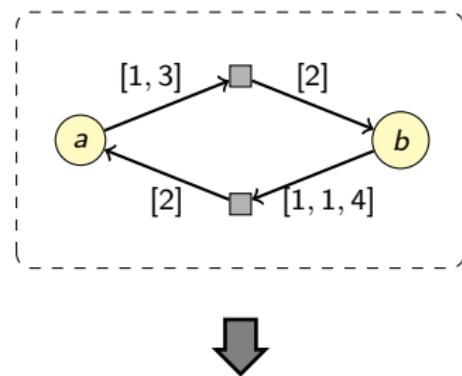
## Synchronous Data Flow

- Fixed behavior
- Periodically repeating



## Cyclo-Static Data Flow

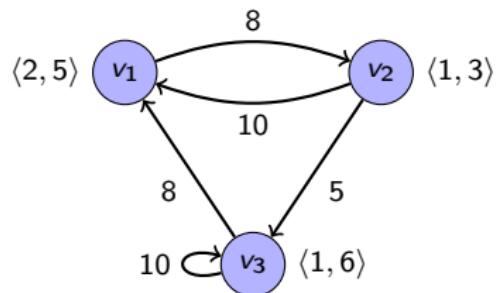
- Changing behavior
- Repeating pattern



The Digraph Real-Time task model.

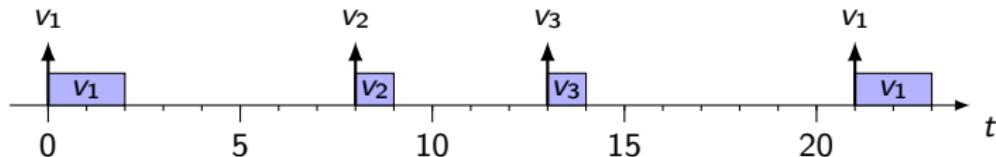
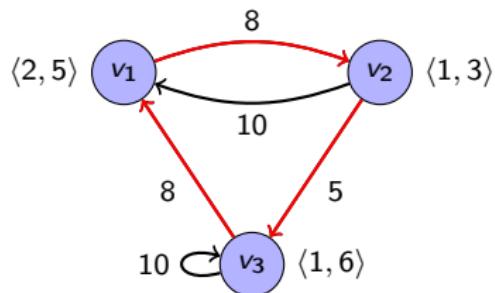
# The Digraph Real-Time (DRT) Task Model

- A graph-based representation
- Different job types



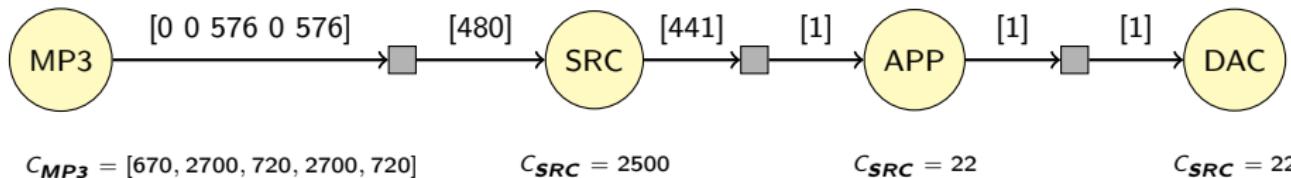
# The Digraph Real-Time (DRT) Task Model

- A graph-based representation
- Different job types

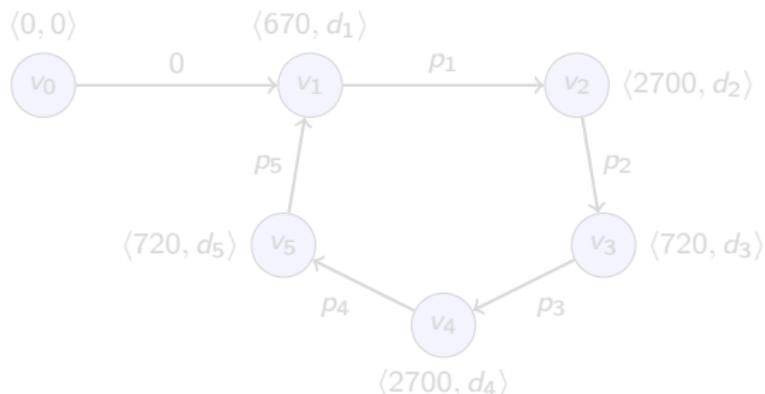


# Example

- MP3 playback application

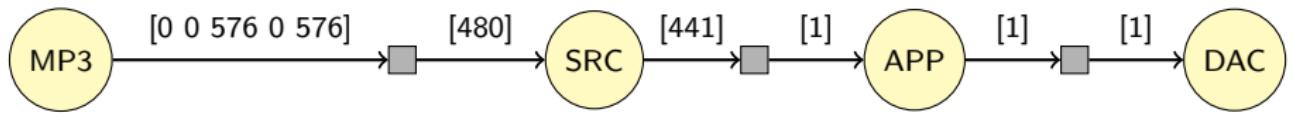


- DRT task for the actor MP3



# Example

- MP3 playback application



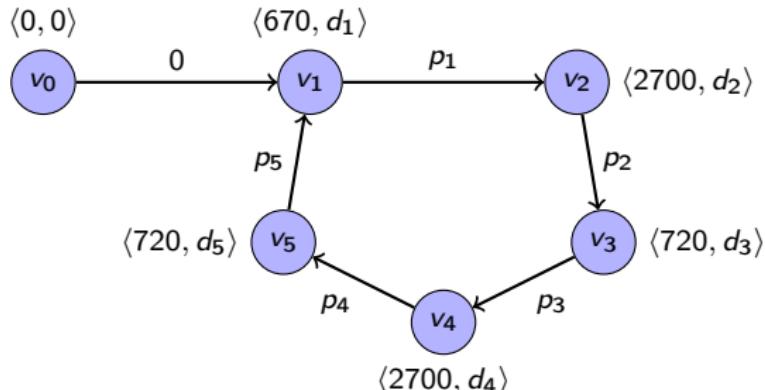
$$C_{MP3} = [670, 2700, 720, 2700, 720]$$

$$C_{SRC} = 2500$$

$$C_{APP} = 22$$

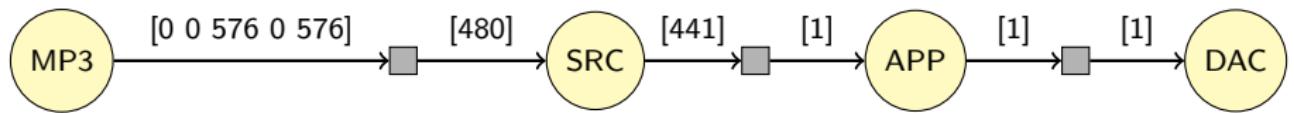
$$C_{DAC} = 22$$

- DRT task for the actor MP3



# Example

- MP3 playback application



$$C_{MP3} = [670, 2700, 720, 2700, 720]$$

$$C_{SRC} = 2500$$

$$C_{SRC} = 22$$

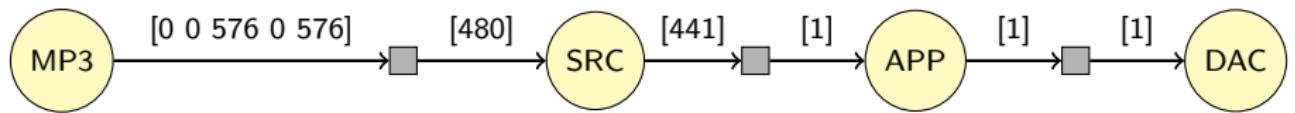
$$C_{SRC} = 22$$

- DRT task for the actor SRC



# Example

- MP3 playback application



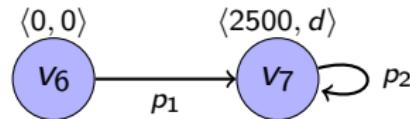
$$C_{MP3} = [670, 2700, 720, 2700, 720]$$

$$C_{SRC} = 2500$$

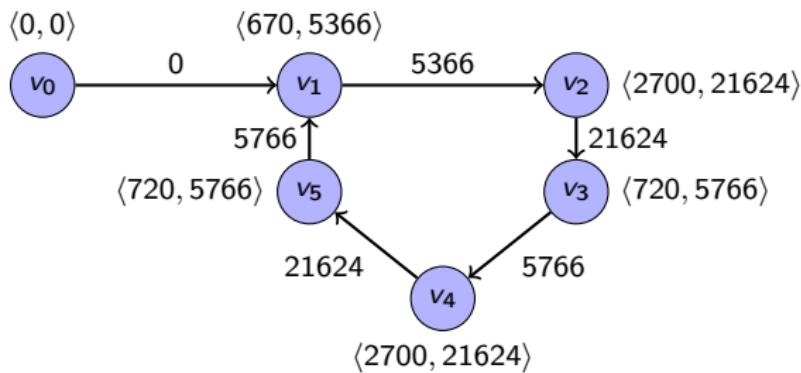
$$C_{SRC} = 22$$

$$C_{SRC} = 22$$

- DRT task for the actor SRC



# Obtained DRT tasks



**Table:** Task set parameters for the DRT tasks ( $\mu s$ )

	Period	Offset
SRC	25061.809	60649.578
APP	56.829	110801.612
DAC	56.829	110943.686

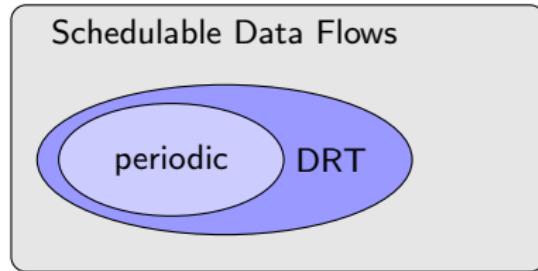
# Evaluation Results

Table: Total buffer requirement and throughput for each method

	Buffer Requirement	Throughput ( $s^{-1}$ )
Periodic Task Set	2273	16013
DRT Task Set	2155	17596
Improvement	5%	9.8%

# Conclusion

- Using a more general task model
  - More flexibility
  - Larger state-space



- Linear approximation

# Modeling and Analysis of Data Flow Graphs using the Digraph Real-Time Task Model

Morteza Mohaqeqi, Jakaria Abdullah, and Wang Yi

Uppsala University

Ada-Europe 2016

*Thanks!*

